

GDH sum rule experiments  
at  $Q^2 = 0$   $\text{GeV}^2/c^2$

@ Spin discussion

July 30, 2002

Tsuneo KAGEYA

LEGS at BNL and Virginia Polytechnic  
Institute and State University

## GDH sum rule $\star$

\* Forward Compton scattering amplitude of GGT

$$A(\omega) = f(\omega) \vec{\epsilon}' \cdot \vec{\epsilon} + i \omega g(\omega^2) \sigma (\vec{\epsilon}' \times \vec{\epsilon})$$

$$g(\omega) = g(0) + g'(0) \omega^2 + O(\omega^4)$$

\* GGT dispersion relation

$$g(0) - g(\infty) = 1/4\pi^2 \int_{\omega_0}^{\infty} (\sigma_{1/2} - \sigma_{3/2})/\omega d\omega$$

\* Low energy theorem of LGG

$$g(0) = -\alpha \kappa^2 / 2m^2$$

\* An assumption

$$g(\infty) = 0$$

$$* \text{GDH} = \int_{\omega_0}^{\infty} (\sigma_{1/2} - \sigma_{3/2})/\omega d\omega$$

$$= -2\pi^2 \alpha \kappa^2 / m^2 - 4\pi^2 g(\infty)$$

(GGT: Gell-Mann, Goldberger & Thirring

Phy. Rev. 95, 1612 (1954)

LLG: Low, Gell-Mann & Goldberger

Phy. Rev. 96, 1428 (1954), 1433 (1954))

$\star$  S. D. Drell & A. C. Hearn, PRL. 16 (1966) 908

S. B. Gerasimov, Yad. Fiz. 2 (1965) 598,

Sov. J. NP. 2 (1966) 430

**Multipole predictions  
for the forward spin-polarizability and the GDH sum rules**

$$\gamma_o = \int \frac{1}{4\pi^2} \frac{\sigma_{\frac{1}{2}} - \sigma_{\frac{3}{2}}}{E_\gamma^3} \quad \text{GDH} = \int \frac{\sigma_{\frac{1}{2}} - \sigma_{\frac{3}{2}}}{E_\gamma}$$

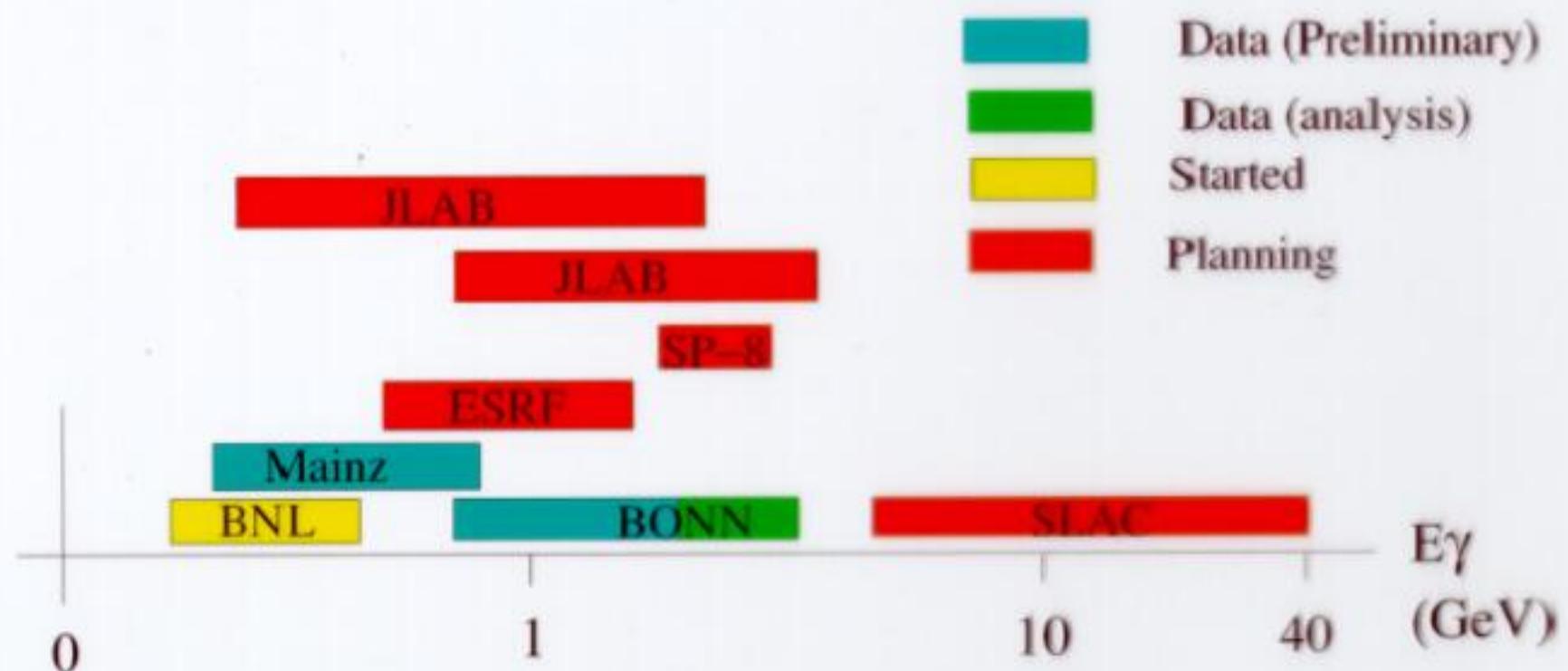
Before the polarized data from Mainz

(a) proton:	$\chi\text{PT}$ rel $O(p^3)$	$HB\chi\text{PT}$ $O(p^4)$	$\pi\text{-multipoles}$ (LEGS+SAID)	<i>GDH predictions</i>
				$-(\kappa_p^2) \frac{2\pi^2\alpha}{m^3}$
$\gamma_o(p) \ (10^{-6} \text{ fm}^4) :$	-150	-100	-155 ( $\pm 15$ )	
$GDH_p \ (10^{-4} \text{ fm}^2) :$			-290 ( $\pm -12$ )	-204

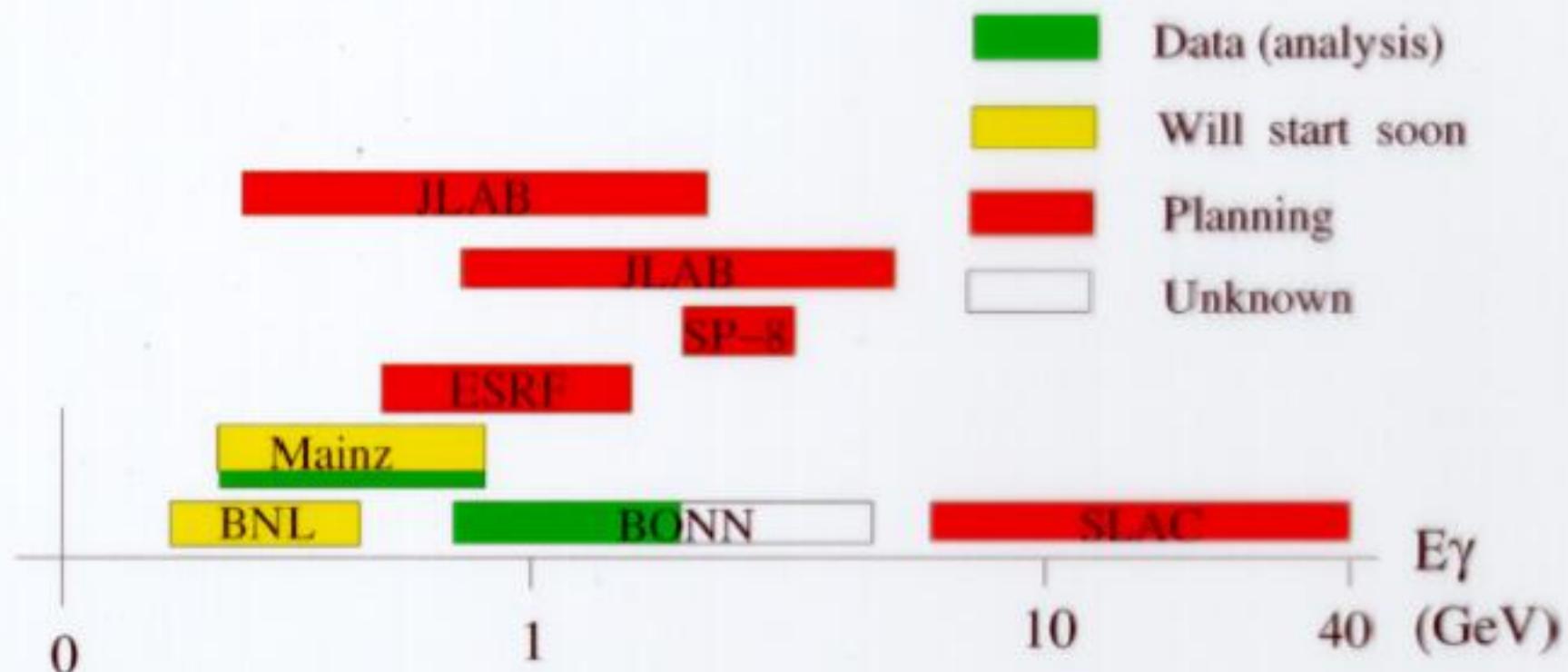
(b) neutron:	$\chi\text{PT}$ rel $O(p^3)$	$HB\chi\text{PT}$ $O(p^4)$	$\pi\text{-multipoles}$ (SAID)	<i>GDH</i>
				$-(\kappa_n^2) \frac{2\pi^2\alpha}{m^3}$
$\gamma_o(n) \ (10^{-6} \text{ fm}^4) :$	-46	+120	-38 ( $\pm -20$ )	
$GDH_n \ (10^{-4} \text{ fm}^2) :$			-160 ( $\pm -16$ )	-234

- note:
- multipole uncertainties reflect propagation of errors on existing data,
  - appropriate for interpolation,
  - may not be good for *extrapolation* to  $\sigma_{1/2}$  and  $\sigma_{3/2}$ .

# Proton GDH experiments at $Q^2 = 0$



# Neutron GDH experiments at $Q^2 = 0$



Mainz & Bonn

J. Ahrens<sup>1</sup>, S. Altieri<sup>13</sup>, J.R.M. Annand<sup>6</sup>, G. Anton<sup>4</sup>, H.-J. Arends<sup>1</sup>,  
G. Audit<sup>15</sup>, R. Beck<sup>1</sup>, C. Bradtke<sup>3</sup>, A. Braghieri<sup>13</sup>, N. d'Hose<sup>15</sup>,  
D. Drachsel<sup>1</sup>, H. Dutz<sup>2</sup>, B. Fürst<sup>1</sup>, S. Goertz<sup>3</sup>, P. Grabmayr<sup>16</sup>,  
S.J. Hall<sup>6</sup>, K. Hansen<sup>8</sup>, J. Harmsen<sup>3</sup>, D. v.Harrach<sup>1</sup>, S. Hasegawa<sup>12</sup>,  
T. Hasegawa<sup>10</sup>, T. Hehl<sup>16</sup>, E. Heid<sup>1</sup>, W. Hell<sup>9</sup>, K. Helbing<sup>4</sup>,  
H. Holvoet<sup>5</sup>, L. van Hoorebeke<sup>5</sup>, N. Horikawa<sup>12</sup>, T. Iwata<sup>12</sup>,  
P. Jennewein<sup>1</sup>, T. Kageya<sup>12</sup>, B. Kiel<sup>1</sup>, F. Klein<sup>2</sup>, R. Kondratjev<sup>11</sup>,  
K. Kossett<sup>7</sup>, J. Krimmer<sup>16</sup>, M. Lang<sup>1</sup>, B. Lannoy<sup>5</sup>, R. Leukel<sup>1</sup>,  
V. Linin<sup>11</sup>, T. Matsuda<sup>10</sup>, J.C. McGeorge<sup>6</sup>, A. Meier<sup>3</sup>, D. Menze<sup>2</sup>,  
W. Meyer<sup>3</sup>, T. Michel<sup>4</sup>, J. Naumann<sup>1</sup>, R.O. Owens<sup>6</sup>, A. Panzeri<sup>13,14</sup>,  
P. Pedroni<sup>13</sup>, T. Pinelli<sup>13,14</sup>, I. Preobrazenski<sup>1</sup>, S. Proff<sup>7</sup>, E. Radtke<sup>3</sup>,  
T. Reichelt<sup>2</sup>, E. Reichert<sup>9</sup>, G. Reicherz<sup>3</sup>, Ch. Rohlof<sup>2</sup>, D. Ryckbosch<sup>5</sup>,  
F. Sadiq<sup>6</sup>, M. Sauer<sup>16</sup>, B. Schoch<sup>2</sup>, B. Schröder<sup>8</sup>, M. Schumacher<sup>7</sup>,  
B. Seitz<sup>7</sup>, F. Smend<sup>7</sup>, T. Speckner<sup>4</sup>, N. Takabayashi<sup>12</sup>, G. Tamas<sup>1</sup>,  
A. Thomas<sup>1</sup>, R. van de Vyver<sup>5</sup>, A. Wakai<sup>12</sup>, R. Weigelt<sup>4</sup>, W. Weihofen<sup>7</sup>,  
B. Wiegers<sup>2</sup>, F. Wissmann<sup>7</sup>, F. Zapadka<sup>7</sup>, and G. Zeitler<sup>4</sup>.

<sup>1</sup> Institut für Kernphysik, Universität Mainz, Germany

<sup>2</sup> Physikalisches Institut, Universität Bonn, Germany

<sup>3</sup> Institut für Experimentalphysik, Ruhr-Universität Bochum, Germany

<sup>4</sup> Physikalisches Institut, Universität Erlangen-Nürnberg, Germany

<sup>5</sup> Department of Subatomic and Radiation Physics RUG, Gent, Belgium

<sup>6</sup> Department of Physics & Astronomy, University of Glasgow, U.K.

<sup>7</sup> II. Physikalisches Institut, Universität Göttingen, Germany

<sup>8</sup> University of Lund, Department of Physics, S-22362 Lund, Sweden

<sup>9</sup> Institut für Physik der Universität Mainz, Germany

<sup>10</sup> Faculty of Engineering, Miyazaki University, Japan

<sup>11</sup> Institute of Nuclear Research, Academy of Science, Moscow, Russia

<sup>12</sup> Dep. of Physics and CIRSE, Nagoya University, Chikusa-ku, Japan

<sup>13</sup> INFN Sezione di Pavia, Italy

<sup>14</sup> Dipartimento di Fisica Nucleare e Teorica, Università di Pavia, Italy

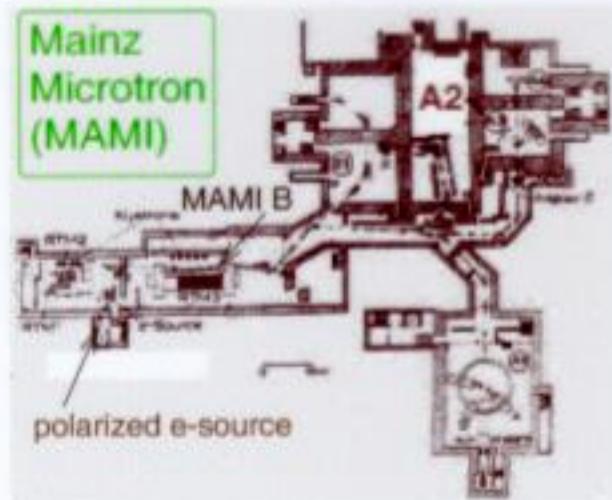
<sup>15</sup> CEA Saclay, DSM/DAPNIA/SPhN, France

<sup>16</sup> Physikalisches Institut, Universität Tübingen, Germany

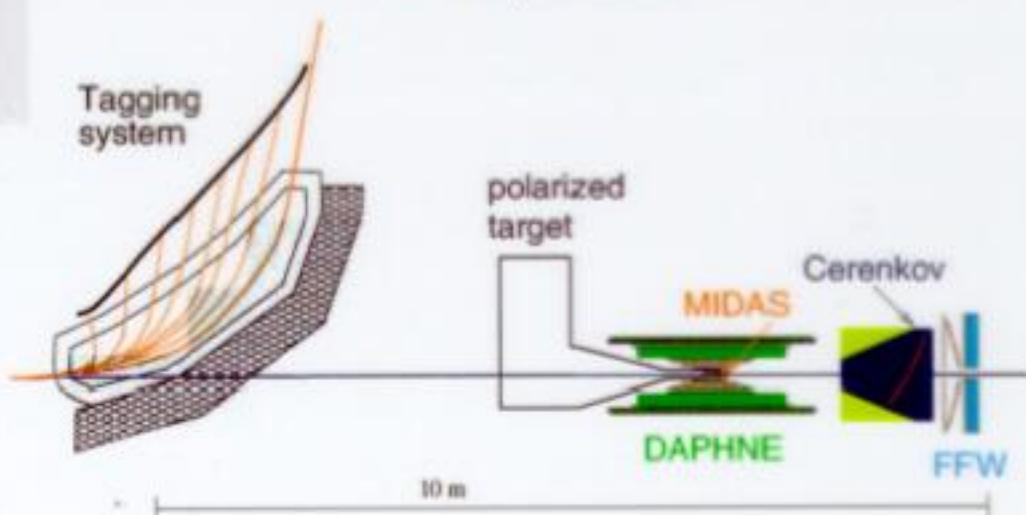


8 countries , 16 institutes

## GDH Facility at MAMI



GDH setup at MAMI



- Existing tagging facility A2
- Photon energy range  
0.14 - 0.8 GeV



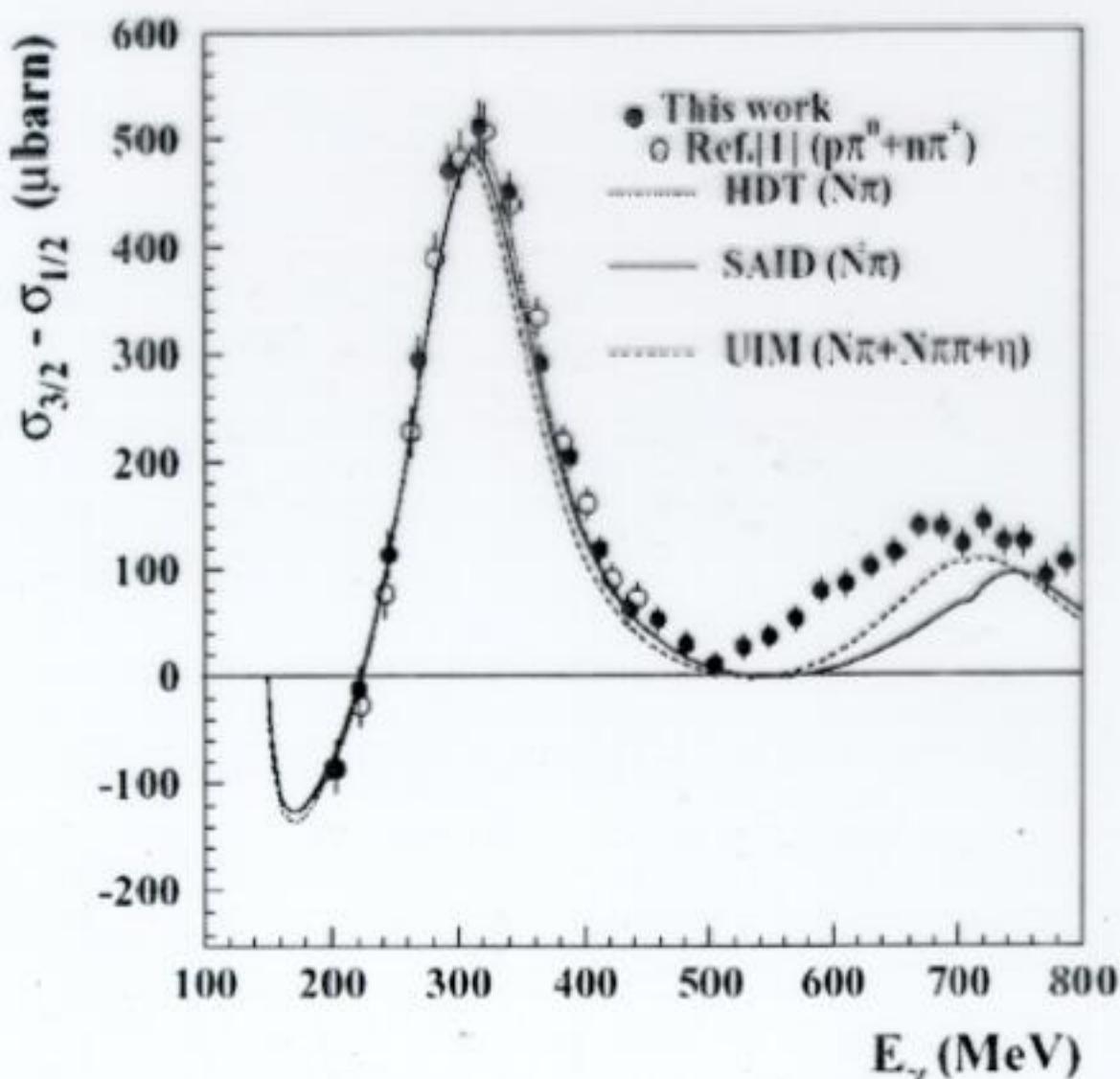
Thomas Jefferson National Accelerator Facility

Operated by the Southeastern Universities Research Association for the U.S. Department of Energy

LATRONIK, July 2-6, 2000, 6

## Mainz GDH result2

Difference of the helicity dependent cross sections for proton



(PRLv87(2001)022003)

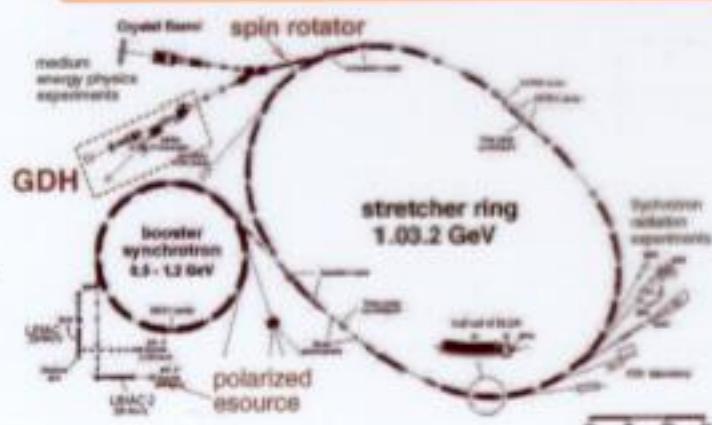
HDT: dispersion theory, Hanstein, Drechsel, Tiator, NPA 632(99), 521

SAID: phenomenological multipole analysis, solution SM99k

UIM: unitary Isobar model, Drechsel, Kamalov, Krein, Tiator, PRD 59(99)

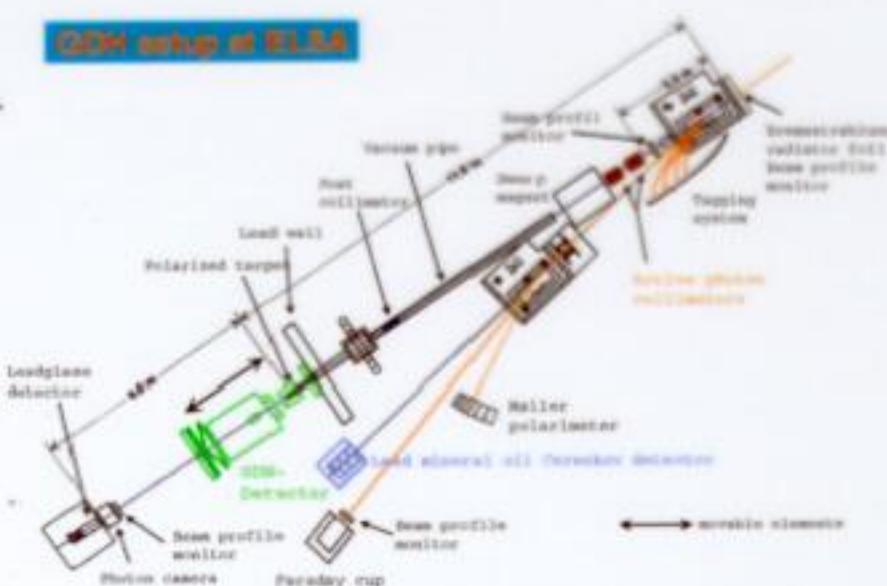
# GDH Facility at ELSA

## Electron Stretcher Accelerator (ELSA)



Grabmayr  
Thursday 14:20

## GDH setup at ELSA



- New experimental area setup for GDH.
- Photon energy range **0.7 - 3.0 GeV**.

Thomas Jefferson National Accelerator Facility

Operated by the Southeastern Universities Research Association for the U.S. Department of Energy

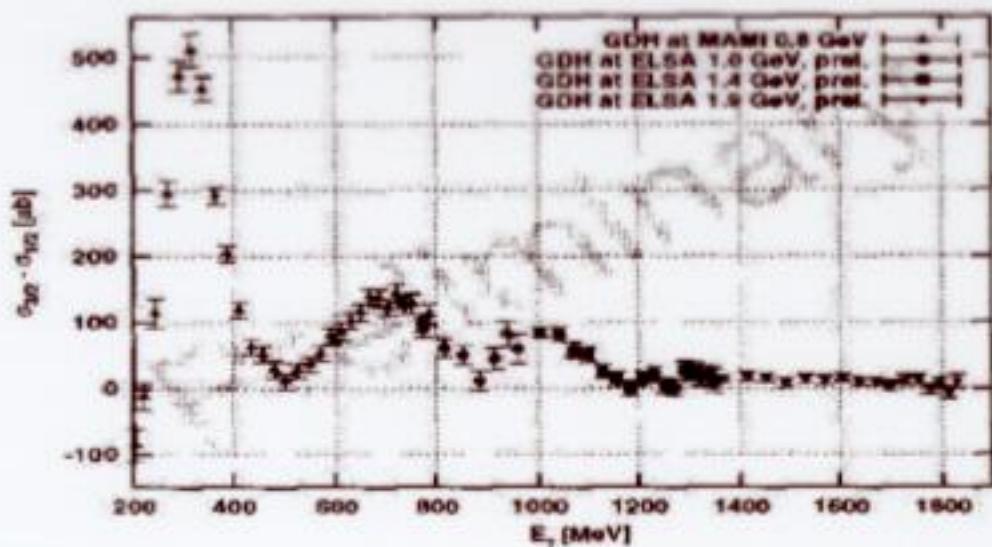
CERN-2000, July 3-6, 2000, 9

# MAMI/ELSA GDH Results at the Proton

Taken from K. Helbing, NPB 105 (2002) 113

MAMI:  $E_\gamma = 200 - 800 \text{ MeV}$

ELSA:  $E_\gamma = 700 - 1850 \text{ MeV}$

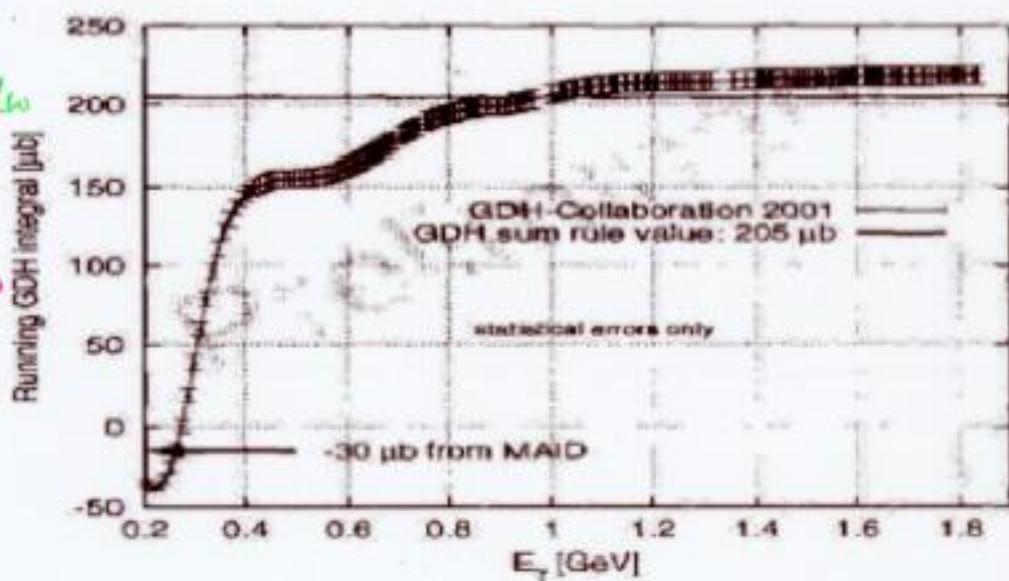


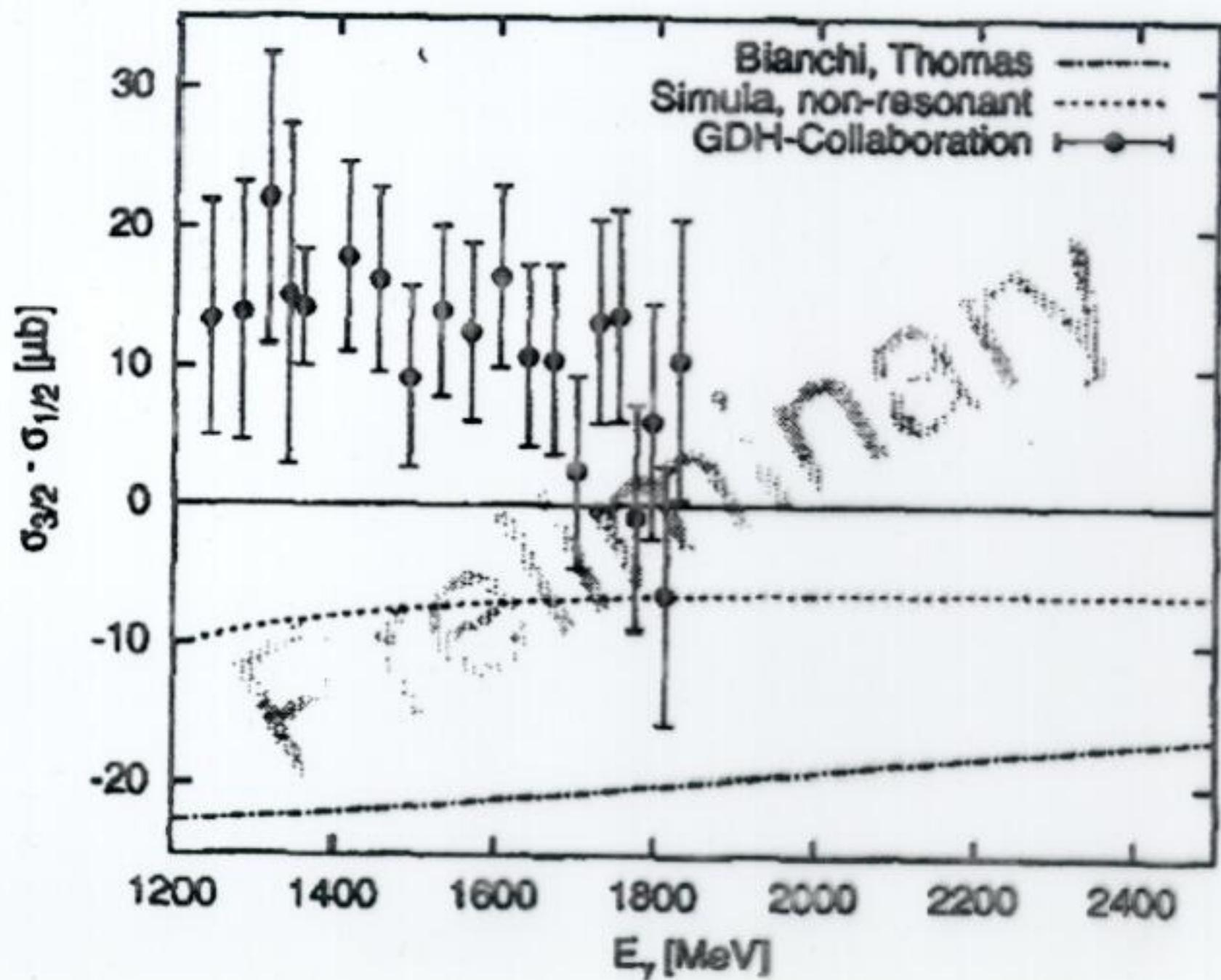
Calculation

$$\int_{\omega_0}^{200 \text{ MeV}} \frac{\partial Y_1 - \partial Y_2}{\omega} d\omega$$

$$+ \int_{200 \text{ MeV}}^{\infty} \frac{\partial Y_1 - \partial Y_2}{\omega} d\omega$$

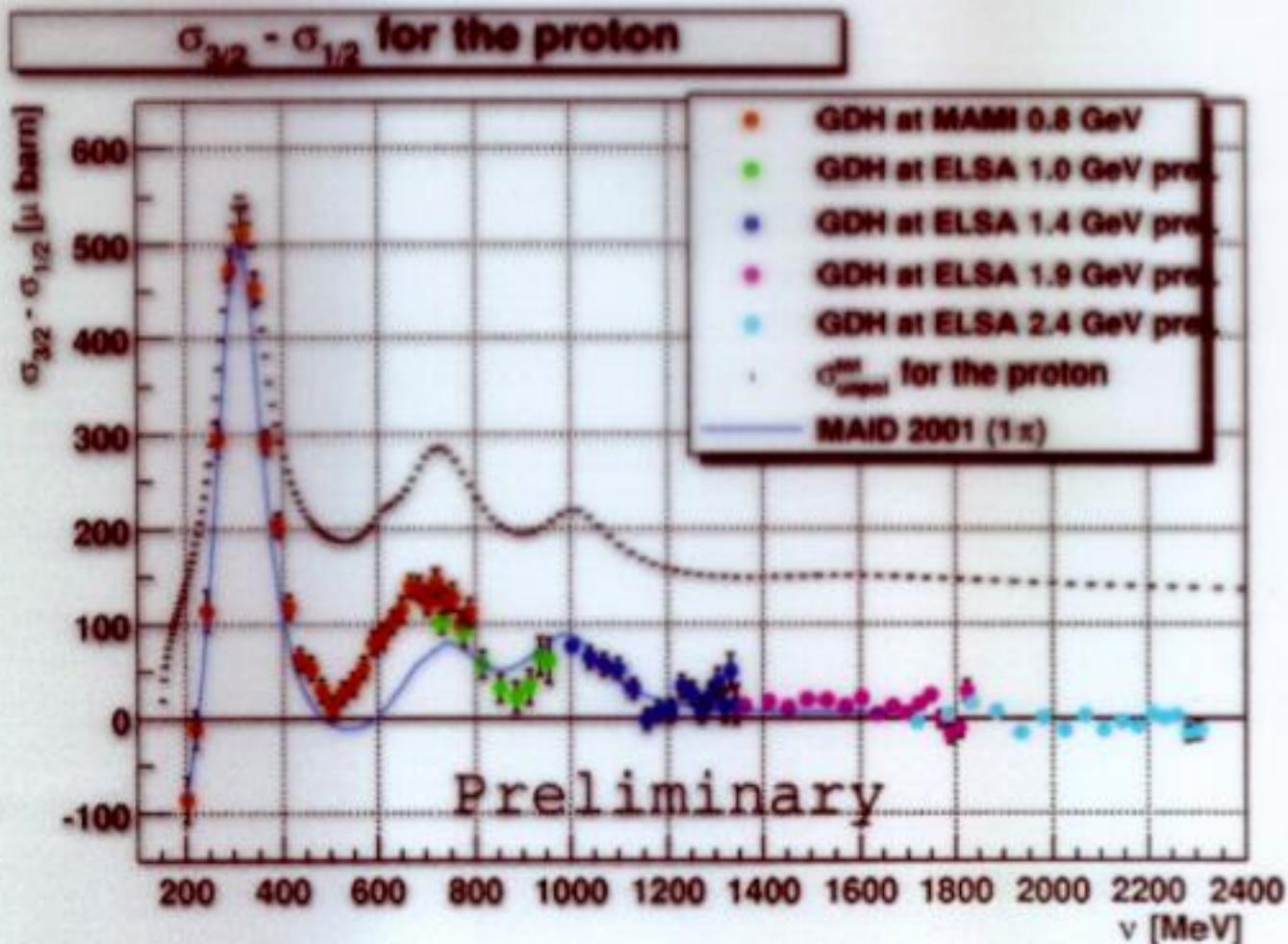
Experiments





## Results for the proton

0.8 – 2.4 GeV



### Comparison of $\sigma_{\text{tot}}$ and $\Delta\sigma$

have structures at similar energies

"pure"  $\Delta$  resonance (M1)

zero  $\Delta\sigma$  between 2<sup>nd</sup> and 3<sup>rd</sup>

for  $E_\gamma > 600$  MeV:  $\sigma_{\text{tot}} = 150 \text{ mb} + \Delta\sigma$

*MAID – Mainz Unitary Isobar Model (Drechsel, Kamalov, Tiator)*  
 – *Tiator, GDH'2000*

**resonance-region  $v = \text{thr} \cdot 1.7 \text{ GeV}$  ( $W < 2 \text{ GeV}$ )**

$$\text{GDH: } I = \int_{\text{thr}}^{1.7 \text{ GeV}} \frac{\sigma_{1/2} - \sigma_{3/2}}{v} dv$$

	proton	neutron	
sum rule:	-204 $\mu\text{b}$	-234 $\mu\text{b}$	◀
Mainz exp. (200-800 MeV)	-218±6	-	
MAID $\gamma, \pi^0$	-150	-154	
MAID $\gamma, \pi^\pm$	-21	+30	!
Mainz $\gamma, \eta$	+15	+10	
Born $\gamma, \pi\pi$ <sup>1)</sup>	-30	-35	
D13 $\gamma, \pi\pi$ <sup>1)</sup>	-15	-15	
sum	-201	-164	
high energy $\gamma, \pi$ <sup>2)</sup>	-4	-4	
$\gamma, K$ <sup>3)</sup>	+4	-2	
total	-201 $\mu\text{b}$	-170 $\mu\text{b}$	◀

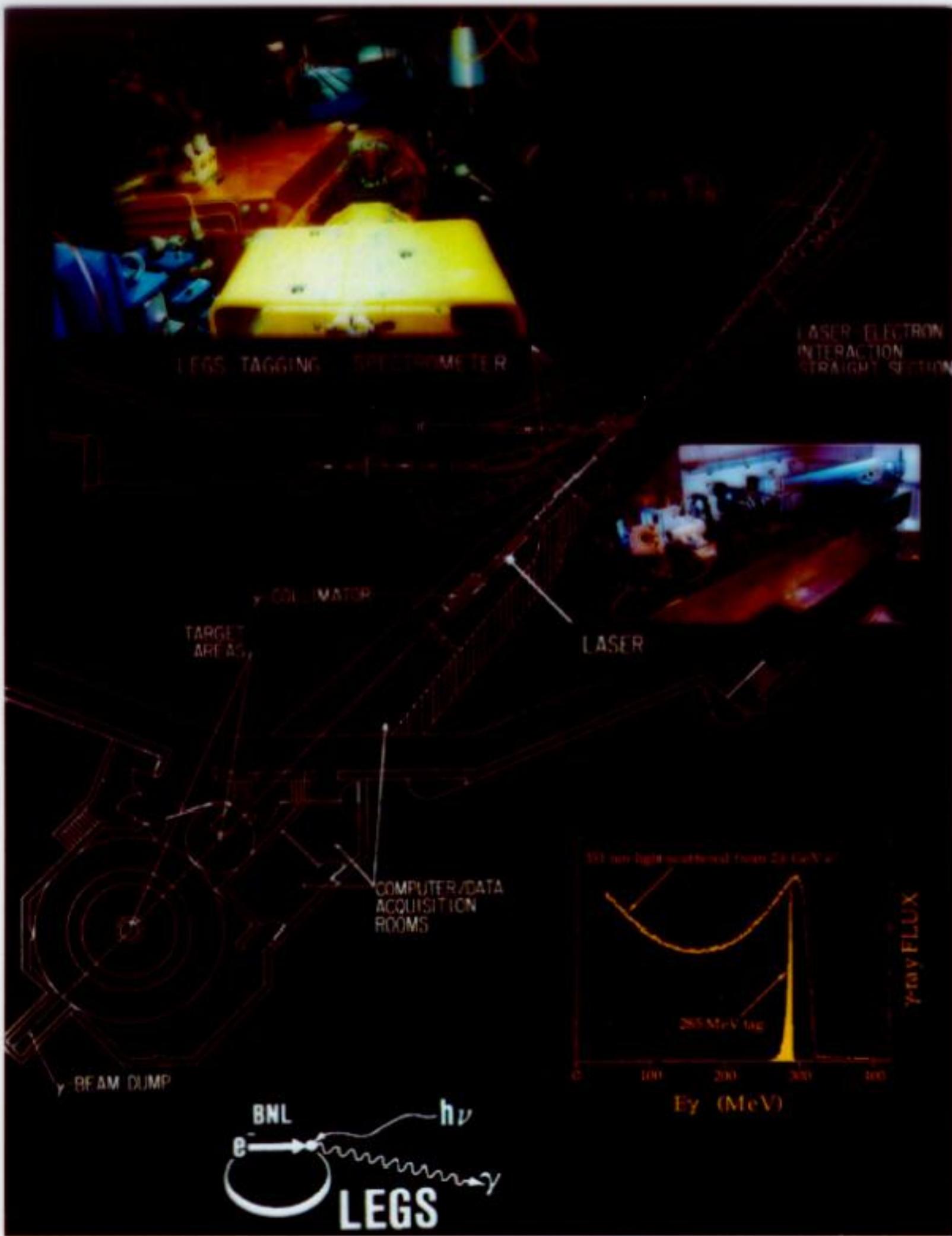
<sup>1)</sup> H. Holvoet and M. Vanderhaeghen in progress

<sup>2)</sup> M. Guidal, J.M. Laget and M. Vanderhaeghen, Nucl. Phys. A 627 (1997) 645

<sup>3)</sup> S. Sumowidago and T. Mart, Phys. Rev. C 60, 028201 (1999)

*"where are the missing -64  $\mu\text{b}$  of the neutron?"*

– *Tiator, GDH'2000*



# LEGS-Spin Collaboration

- Brookhaven National Laboratory
  - *C. Cacace, A. Caracappa, S. Hoblit, O.C. Kistner, A. Kuczewski, F. Lincoln, M. Lowry, L. Miceli, A.M. Sandorfi, C. Thom, X. Wei*
- James Madison University
  - *A. Lehmann, C.S. Whisenant*
- Norfolk State University
  - *M. Khandakar*
- Ohio University
  - *K. Ardashev, C. Bade, R. Deininger, K. Hicks, M. Lucas, J. Mahon*
- Syracuse University
  - *A. Honig*
- Università di Roma II – Tor Vergata
  - *A. D'Angelo, A. d'Angelo, R. Di Salvo, D. Moricciani, C. Schaerf*
- Université de Paris – Sud, ORSAY
  - *C. Commeaux, J.-P. Didelez*
- University of South Carolina
  - *I. Danchev, C. Gibson, B.M. Freedman*
- University of Virginia
  - *A. Cichocki, B. Norum, K. Wang*
- Virginia Polytechnic Institute & State University
  - *M. Blecher, T. Kageya, H. Meyer, T. Saitoh*

3 countries, 10 institutes

## LEGS (Laser Electron Gamma Source) GDH experiments

1. Compton backscattered polarized  $\gamma$  beam

$0.15 < E\gamma < 0.47 \text{ GeV}$

$P\gamma \sim 90 \%$

2. Polarized HD solid target

Good dilution factor

$\overrightarrow{\text{HD}}, \overrightarrow{\text{HD}}$  and  $\overrightarrow{\text{HD}}$

$P_H \sim 80 \%, P_D \sim 50 \%$

3.  $4\pi$  detector

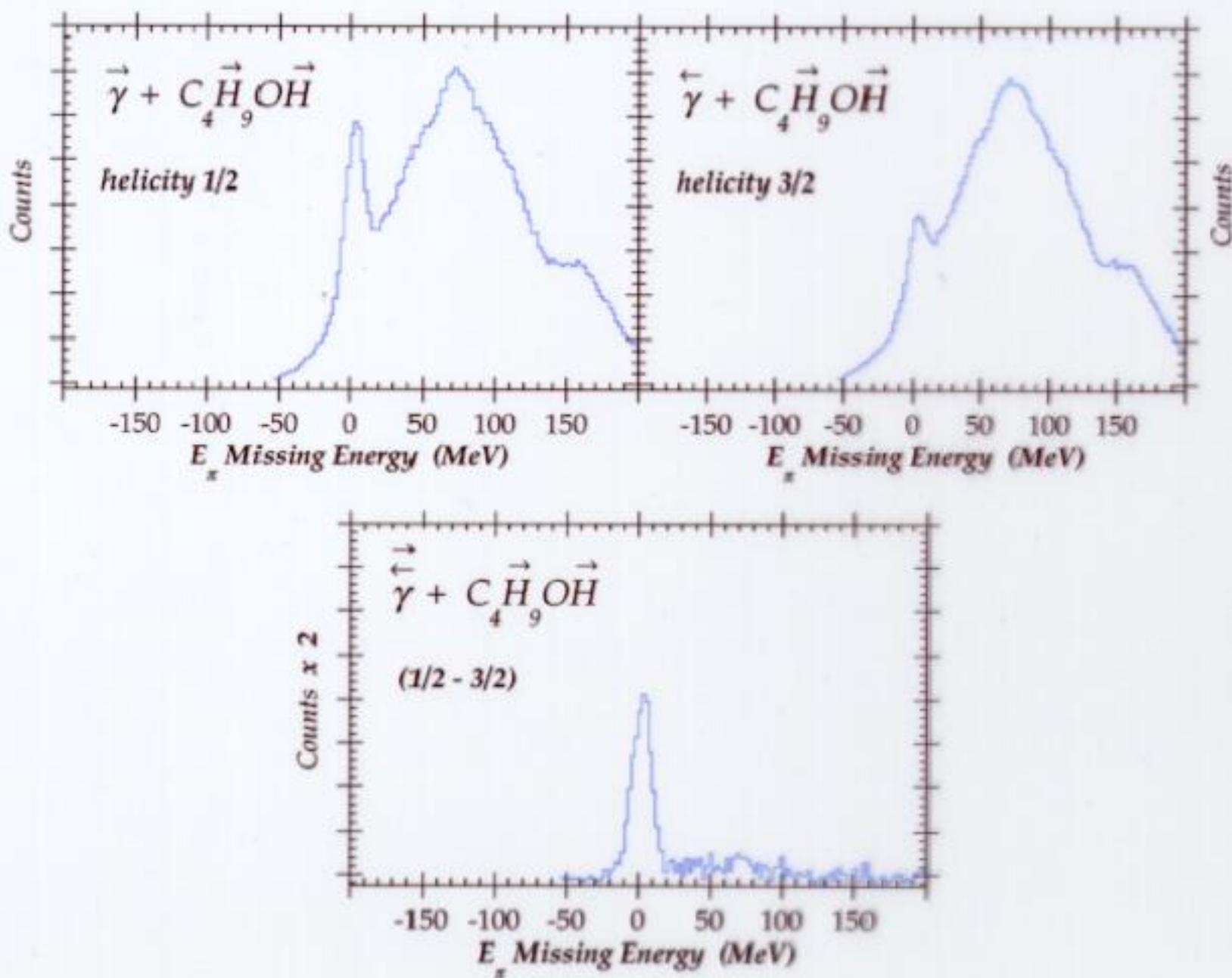
$(\sigma_{1/2} - \sigma_{3/2}) / E\gamma ;$

Total cross sections

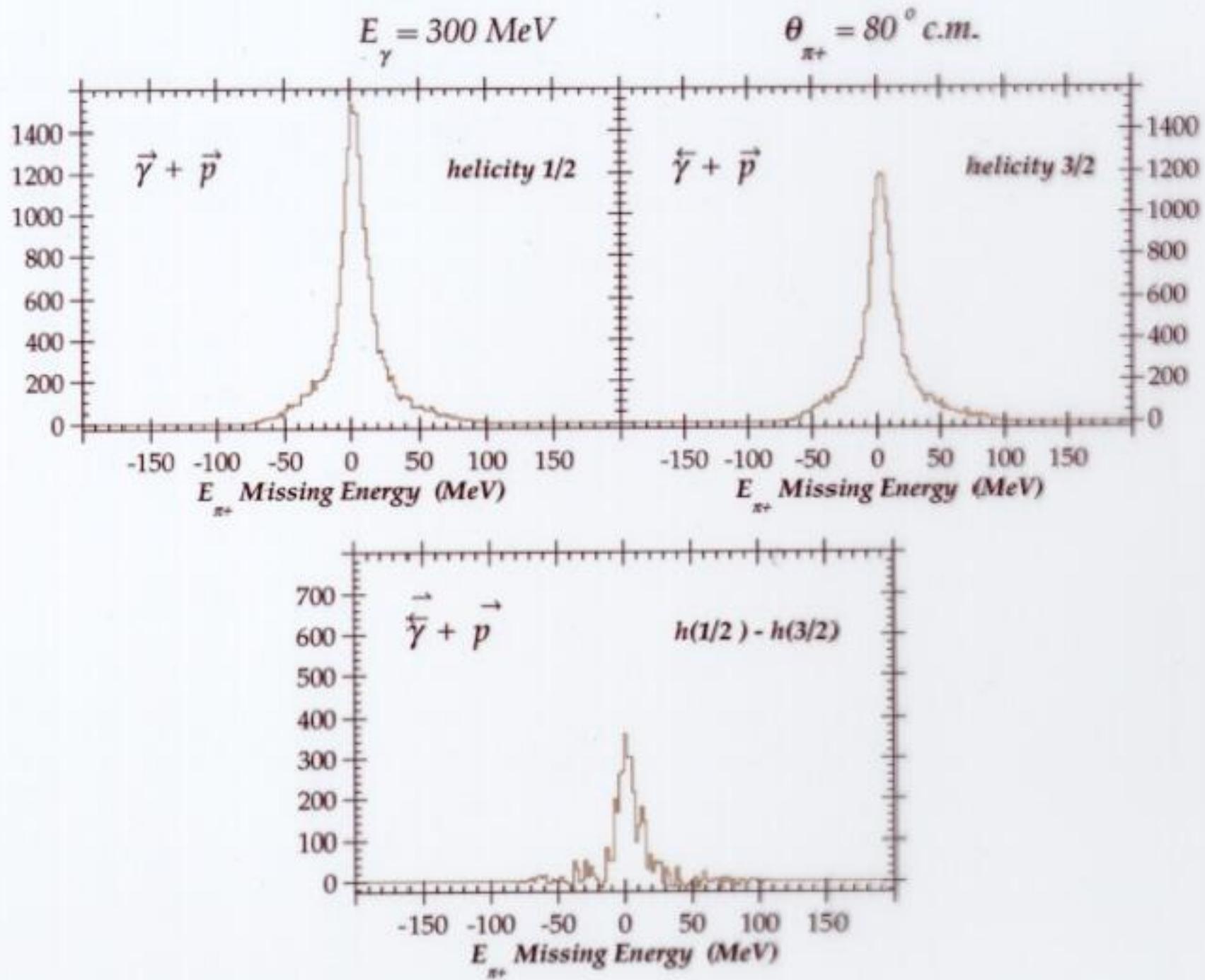
Mainz:  $\gamma + C_4H_9OH \rightarrow p$

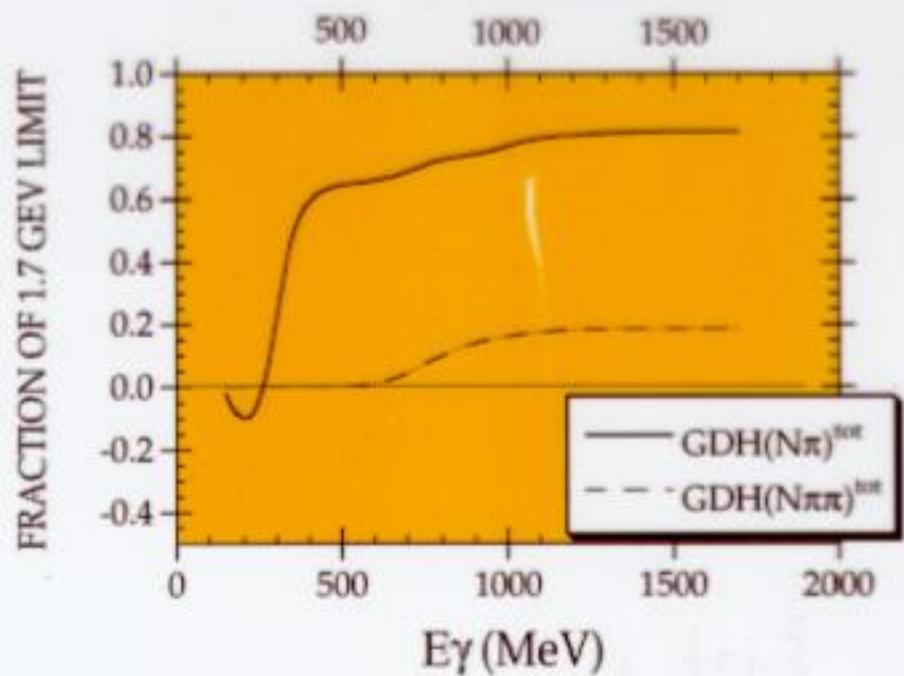
$E_\gamma \sim \Delta$  region

PRL 84(2000)5950

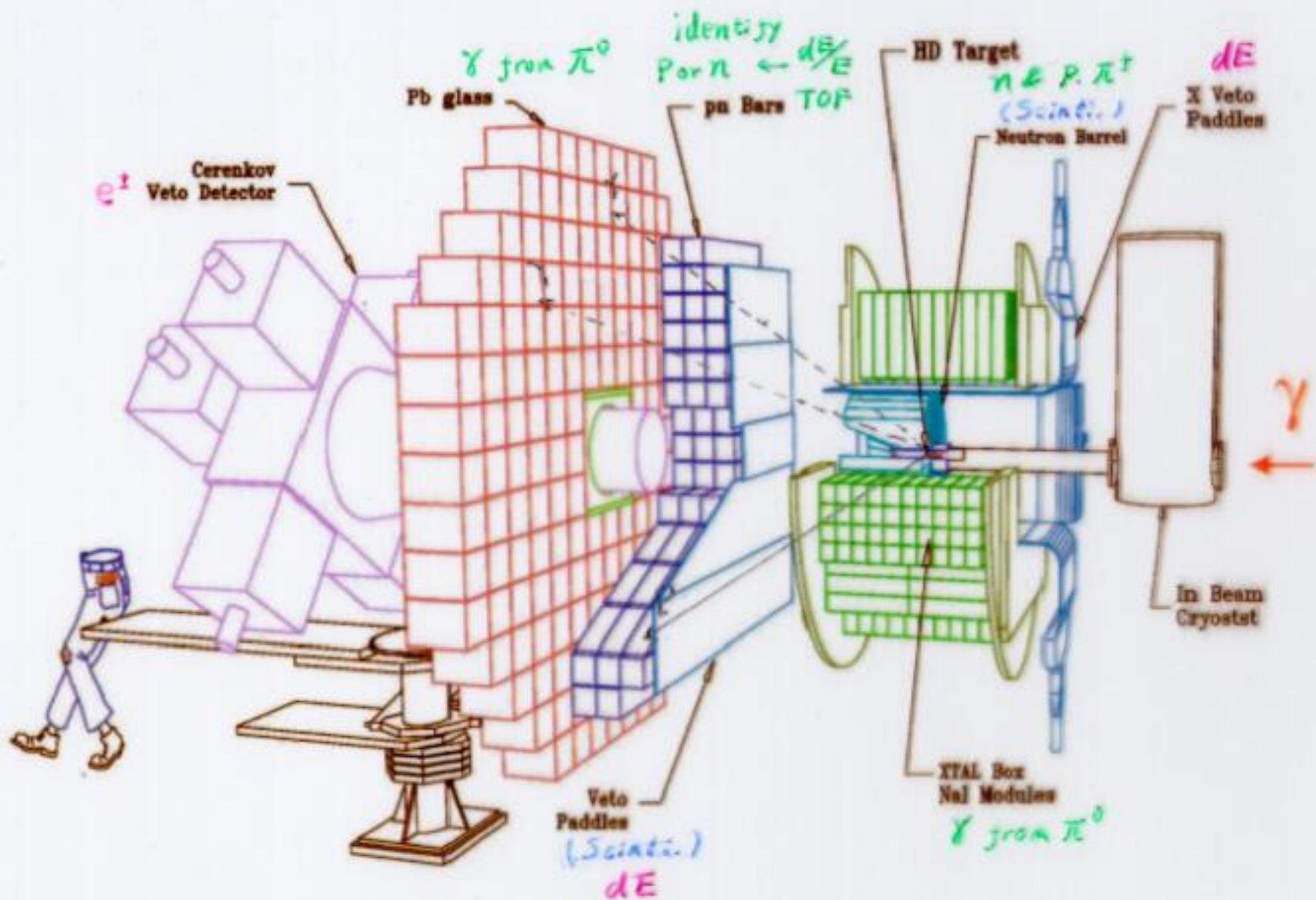


*1st double-polarization data with HD - LEGS/Nov17'01*





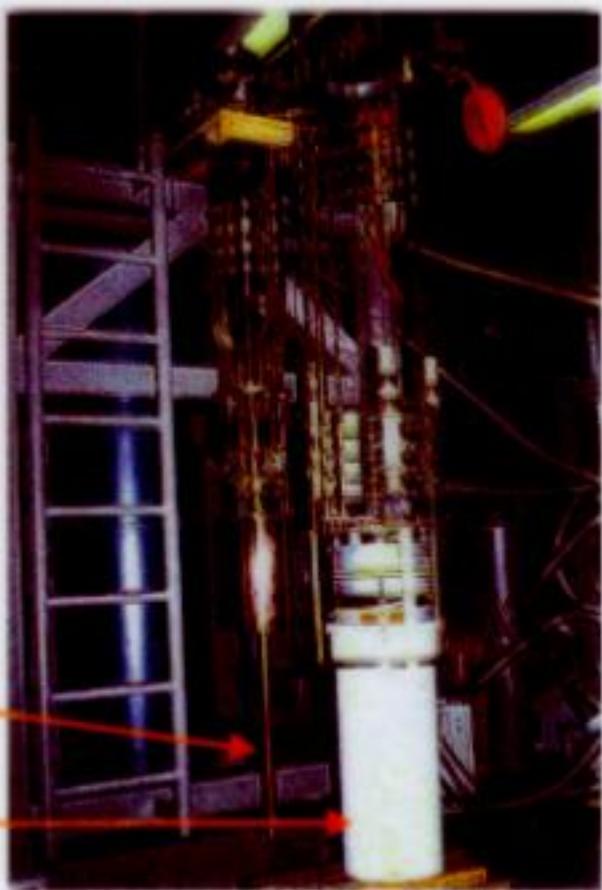
# SASY Current Setup



## *HD target cycle:*



target injection into dilution fridge;  
~50 to 100 days at 15 Tesla / 18 mK

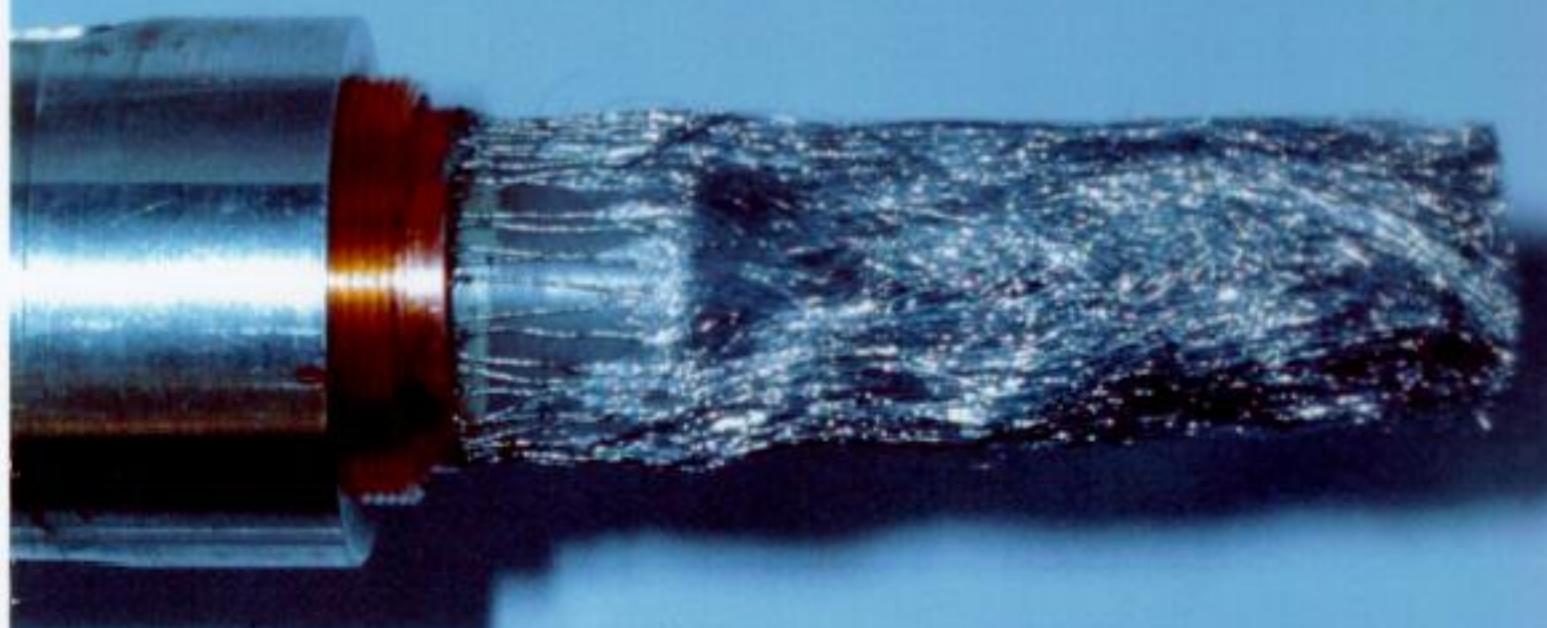


loading in-beam cryostat  
(1.25°K and 0.7 Tesla)

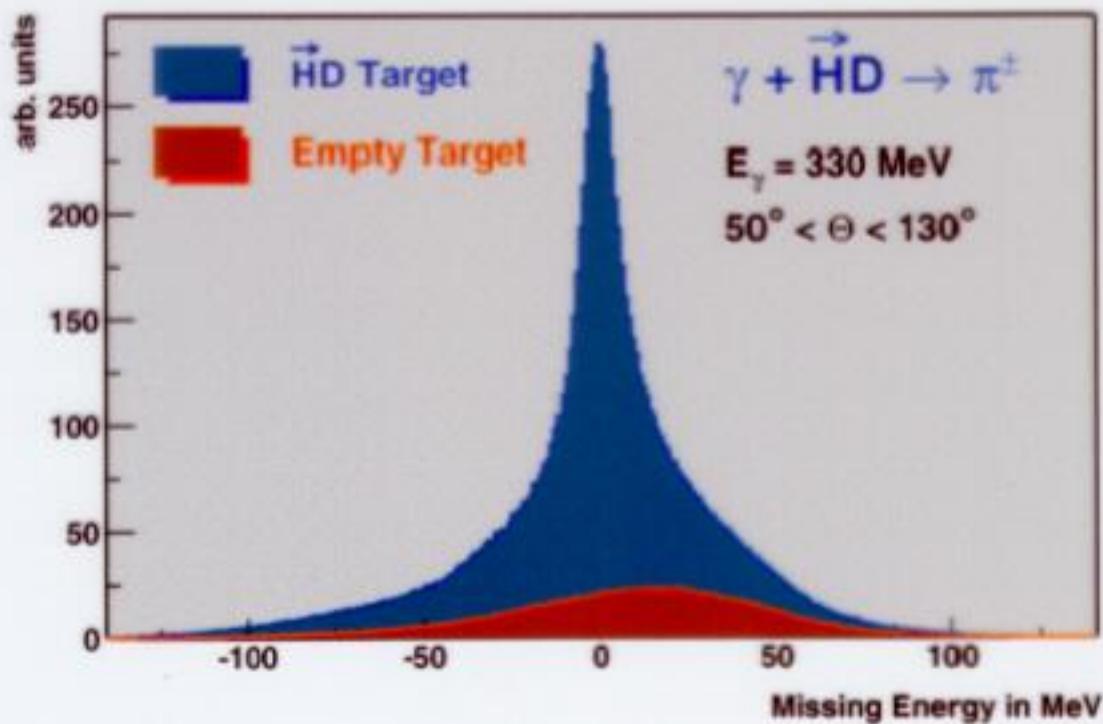


extraction at 2.5°K and 0.016 T





## Empty Target Contribution



area in red is 20% of blue

as expected

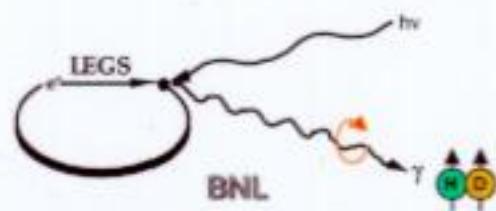
# Target Polarization History

- Initial  $P_T = \begin{cases} 71\% \text{ for H} \\ 16\% \text{ for D} \end{cases}$
- Many tests to study target under various conditions (transfers, different holding fields and temperatures)
- Start conditions in-beam
  - $P_T = \begin{cases} 30 \pm 3\% \text{ for H } (T_1 = 13\text{d}) \\ 6 \pm 1\% \text{ for D } (T_1 = 36\text{d}) \end{cases}$
- Calibration of Polarization:
  - NMR line shift due to polarization decay (change in B field)
  - { low-B/hi-T thermal equilibrium NMR signal ( $H_2 + HD$ ) }
- After 2 days magnet quench  
⇒  $P_T$  dropped by about a factor of two
- After 1.5 days accelerator shutdown

⇒ 3.5 days of net data taking

$$\bar{P}_H = \int (P_H dt) / \int dt = 21.3\%$$

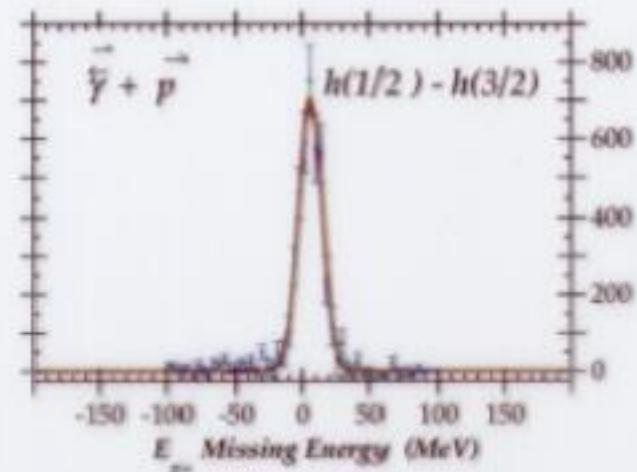
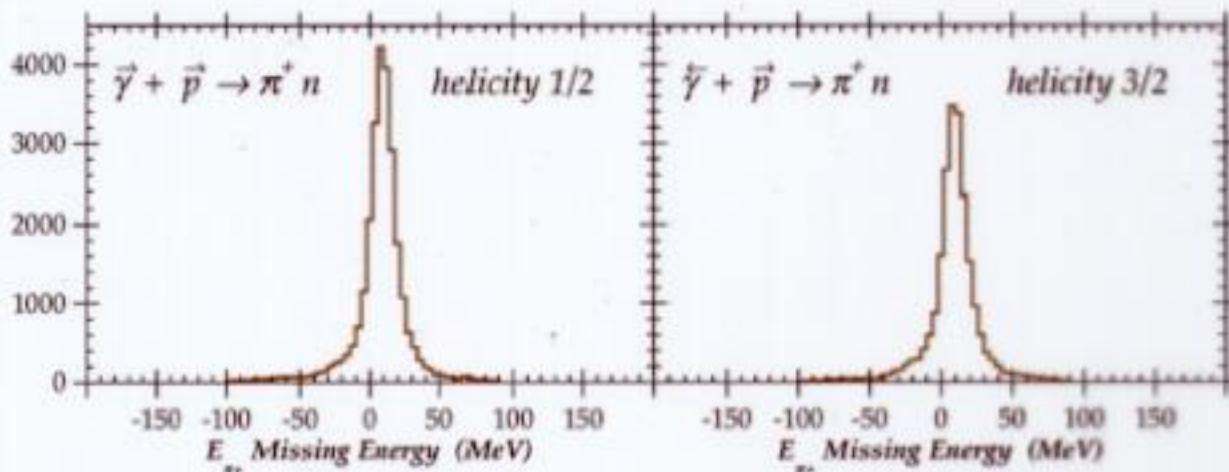
$$\bar{P}_D = \int (P_D dt) / \int dt = 5.0\%$$



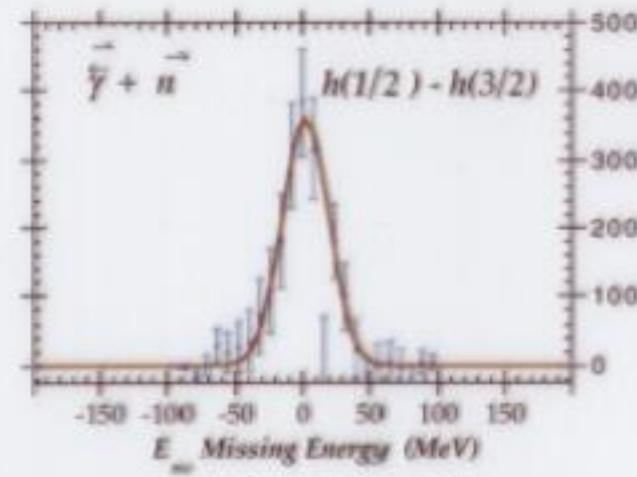
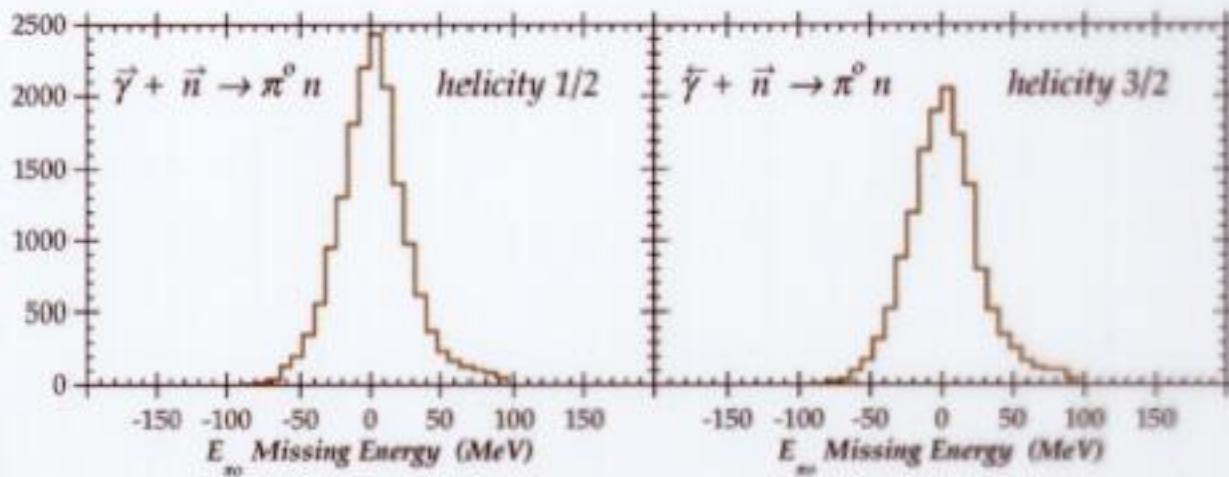
**300 MeV < E $\gamma$  < 350 MeV**

**75° < θ<sub>CM</sub> < 105°**

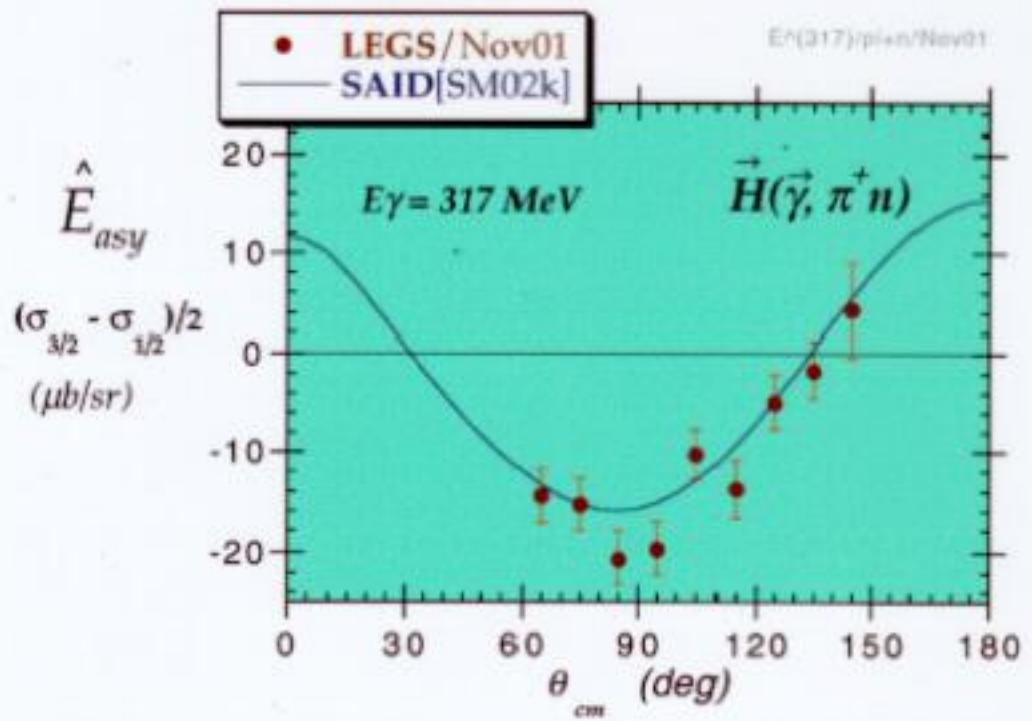
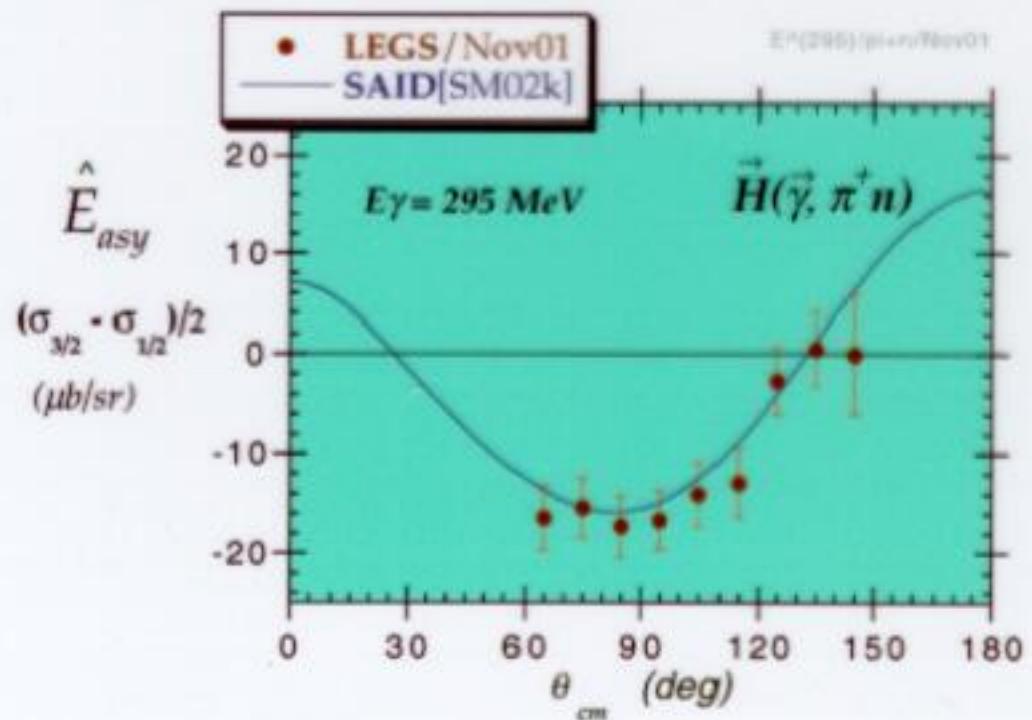
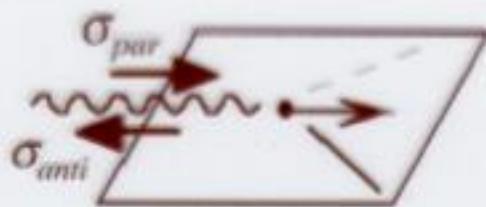
$\rightarrow \rightarrow$   
 $\text{HD}(\vec{\gamma}, \pi^+ n)$



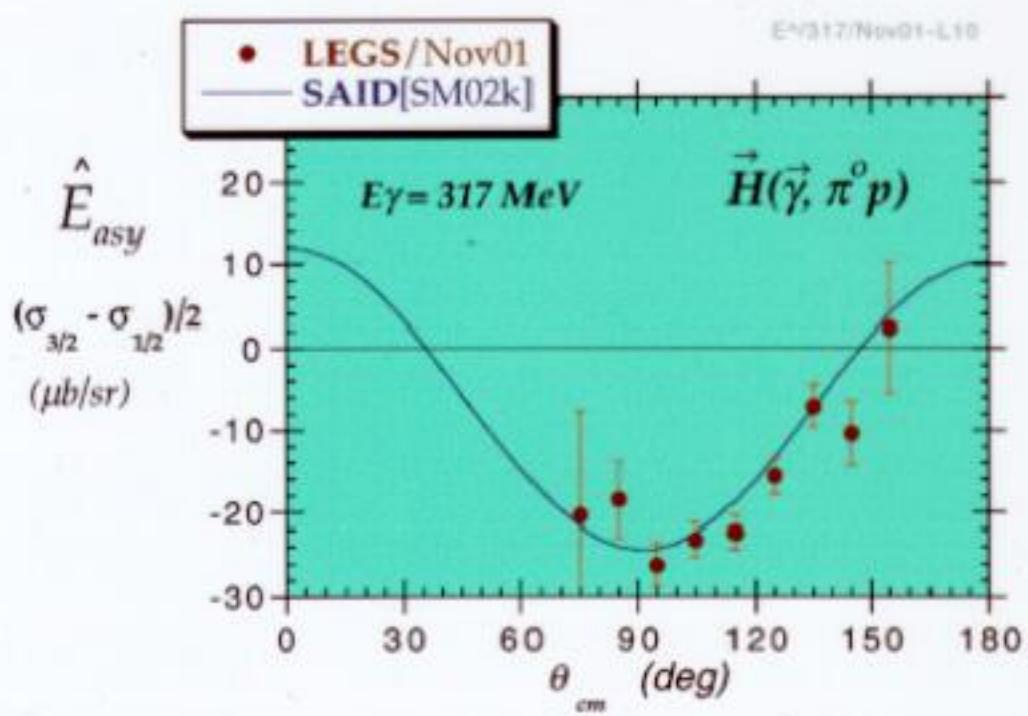
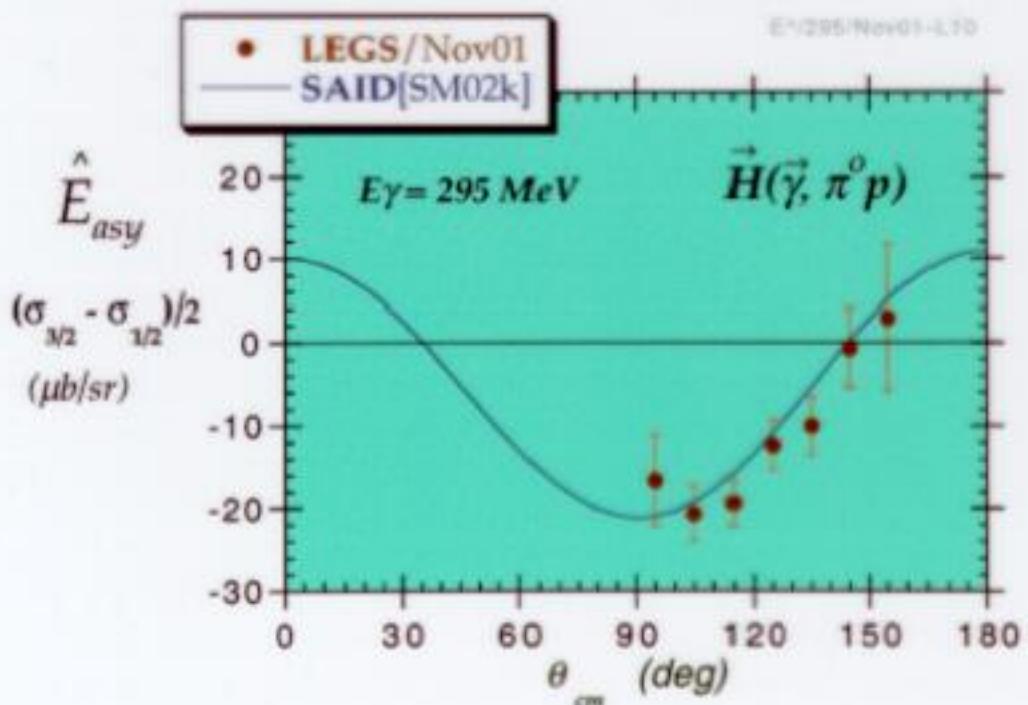
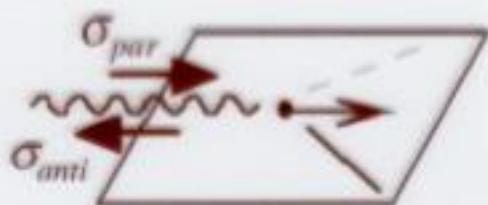
$\rightarrow$   
 $D(\vec{\gamma}, \pi^0 n)$



$$\hat{E}_{asy} = \frac{1}{2}(\sigma_{3/2} - \sigma_{1/2})$$



$$\hat{E}_{asy} = \frac{1}{2}(\sigma_{3/2} - \sigma_{1/2})$$





## GDH Program at LEGS

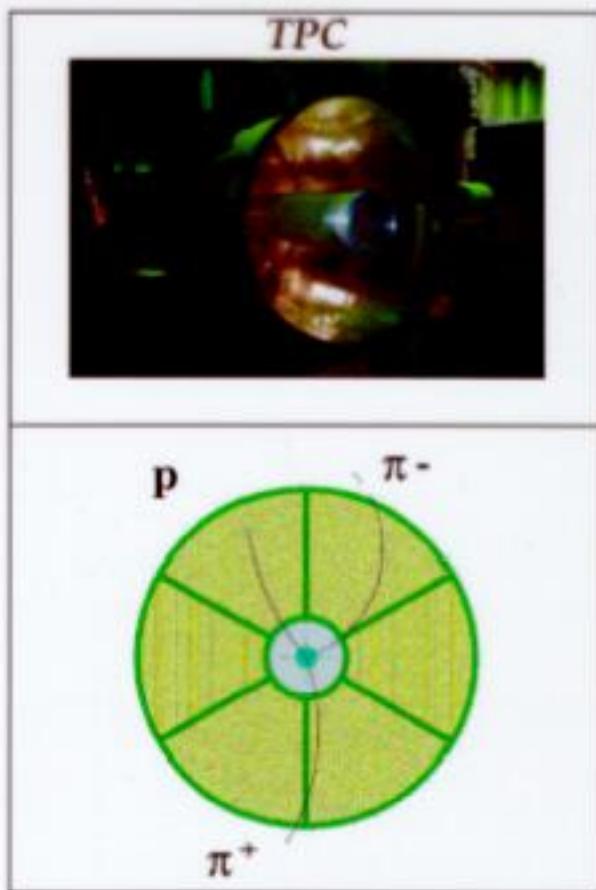
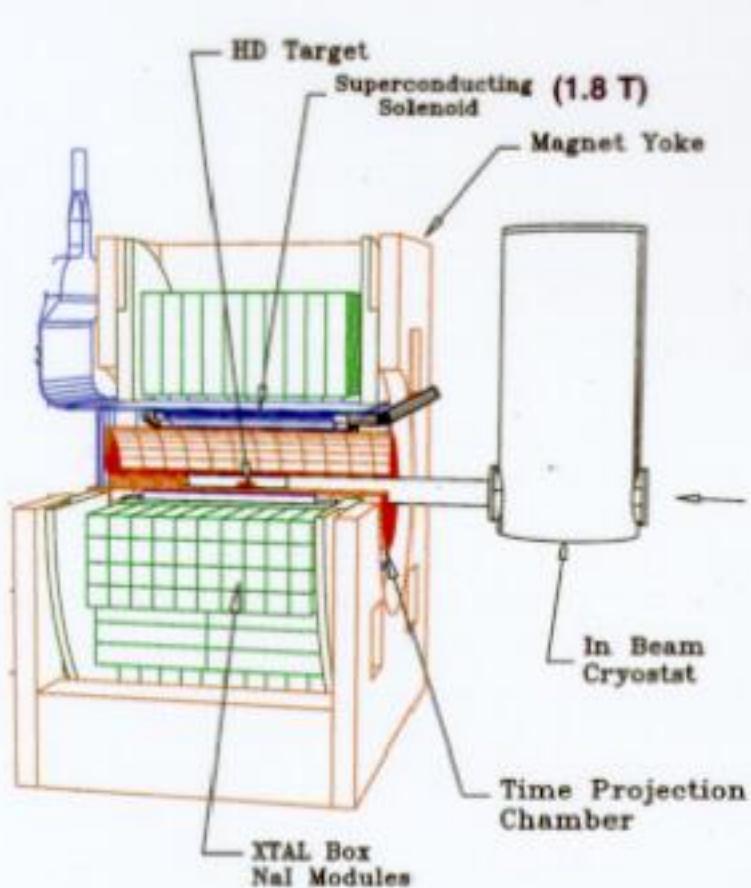
~ threshold  $< E_\gamma < 470$  MeV

### near-term plans:

- polarized-D measurements, focusing on  $\gamma + D \rightarrow \pi^0 n$   
– starting fall'02
- polarized-H measurements  
– starting summer'03

### longer-term plans:

- separate  $D(\gamma, \pi^- p)$  from  $D(\gamma, \pi^+ n)$ :  
isolate  $\gamma + n \rightarrow \pi^- p$  at low energies  $\Leftrightarrow$  measuring the  $\pi^+$  charge  
 $\Rightarrow$  magnetic analysis in a *Time-Projection Chamber (TPC)*



- TPC experiments in 2005



## GDH Program at LEGS

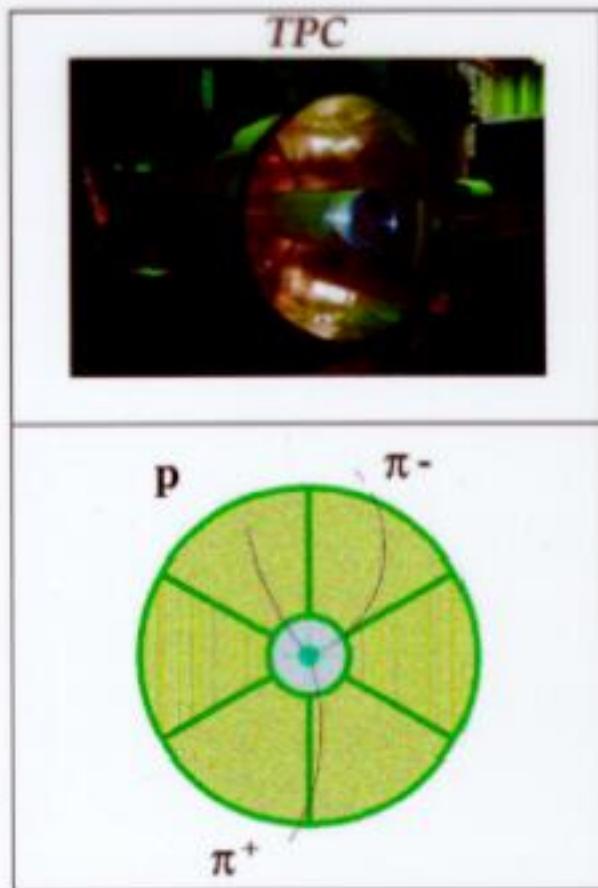
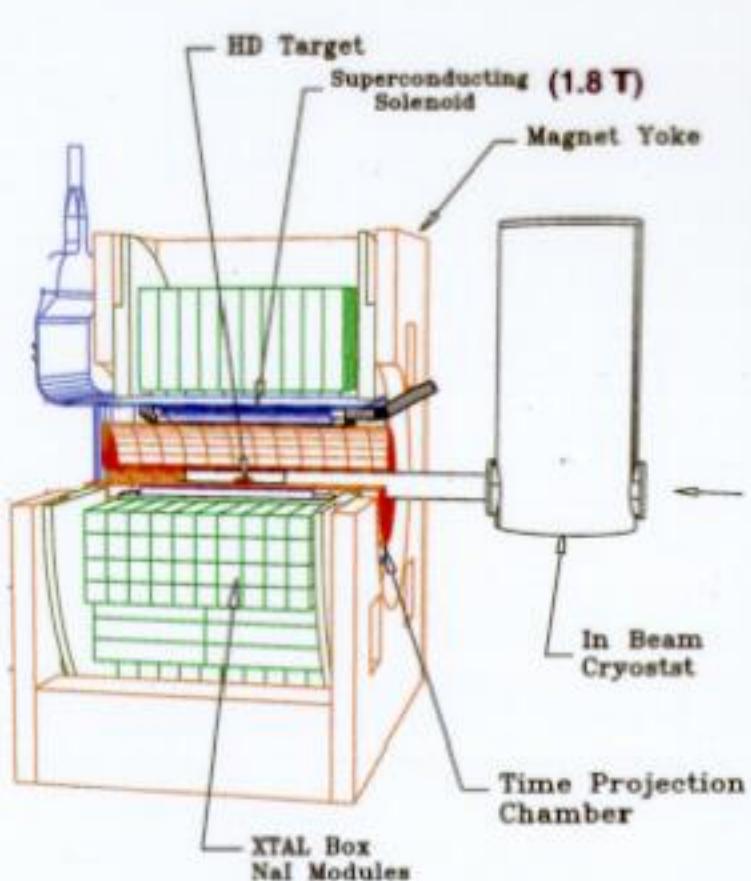
~ threshold  $< E_\gamma < 470$  MeV

### near-term plans:

- polarized-D measurements, focusing on  $\gamma + D \rightarrow \pi^0 n$   
– starting fall'02
- polarized-H measurements  
– starting summer'03

### longer-term plans:

- separate  $D(\gamma, \pi^- p)$  from  $D(\gamma, \pi^+ n)$ :  
isolate  $\gamma + n \rightarrow \pi^- p$  at low energies  $\Leftrightarrow$  measuring the  $\pi^+$  charge  
 $\Rightarrow$  magnetic analysis in a *Time-Projection Chamber (TPC)*



- TPC experiments in 2005

## Future Plans

(1) Improve DF performance at High Field

Vibration isolation from pumping line

- reduce eddy current heating

D polarization  $\rightarrow$  22 %

(2) Forbidden Adiabatic Fast Transition at DF

Install resonance coils in DF

D polarization 22 %  $\rightarrow$  Higher

(3) IBC (Orsay)  $\rightarrow$  New IBC (Quantum tech.)

1.3 K                    0.2 K

0.65 Tesla              1 Tesla

(4) TC (Orsay)  $\rightarrow$  New TC (BNL/Juelich)

0.016 Tesla              0.16 Tesla

(5) Construction of Time Projection Chamber

Identify  $\pi^+/\pi^-$

## Summary

1. Recently **GDH data** started to be taken at  **$Q^2 = 0$**  and small  **$Q^2$**
2. Data with **high quality** and **high statistics** are required to be taken from **pion threshold** to **higher energy** for proton and neutron
3. **Results** are required to be **confirmed** by other experiments **independently**
4. Mainz and Bonn have been taking, will continue to take data and the analyses are going on.
5. LEGS started taking data in November 2001 and plan to **run** for deuteron for a couple of months in **2002, 2003**
6. LEGS will **improve** the **target system** and **design**, construct and install TPC

## Generalized GDH sum rule

\* At  $Q^2 = 0$

$$I_{GDH}(0) \equiv \int_{\omega_*}^{\infty} (\sigma_{1/2} - \sigma_{3/2}) / \omega \, d\omega = -2\pi^2 \alpha \kappa^2 / m^2$$

$$* I_{GDH}(Q^2) = 16\pi^2 \alpha / Q^2 \int_0^1 dx g_1(x, Q^2)$$

(M. Anselmino et al., Sov J. Nuc Phys. 49(1989) 136)

# Relation to $Q^2 > 0$

- From N. Bianchi and E. Thomas, hep-ph/9902266

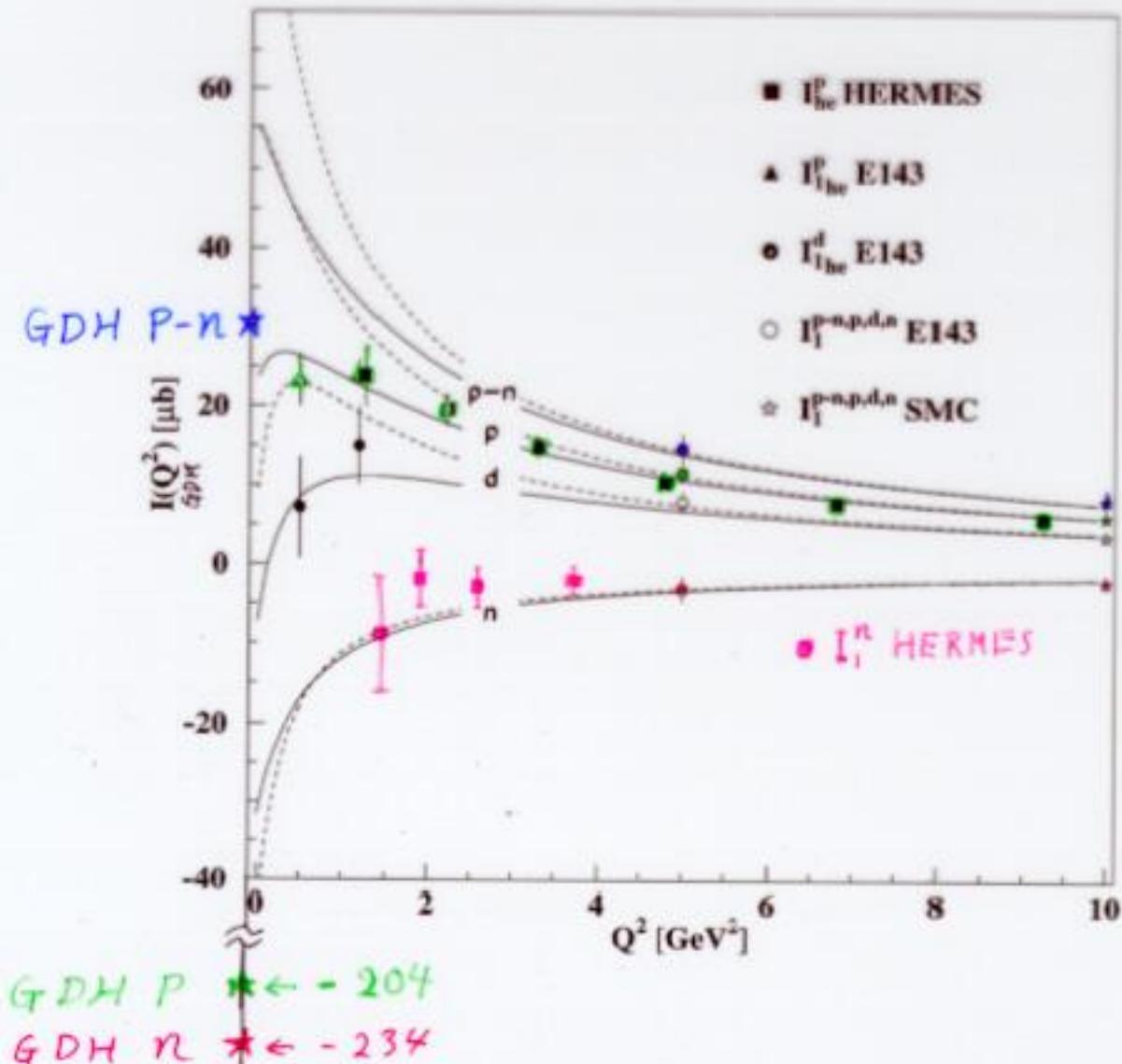


Figure 4:  $Q^2$ -evolution of  $I_{he}(Q^2)$  (solid curves) and of  $I(Q^2)$  (dashed curves) evaluated with Model II for (p-n), p, d and n. The Model predictions are compared with experimental results. The error bars show the quadratic combination of the statistical and the systematic uncertainties.

our measured points by interpolation, or for a few points, extrapolation. The results are plotted in Fig. 2 as a function of  $\nu$ . The prominent peak in the cross section is the

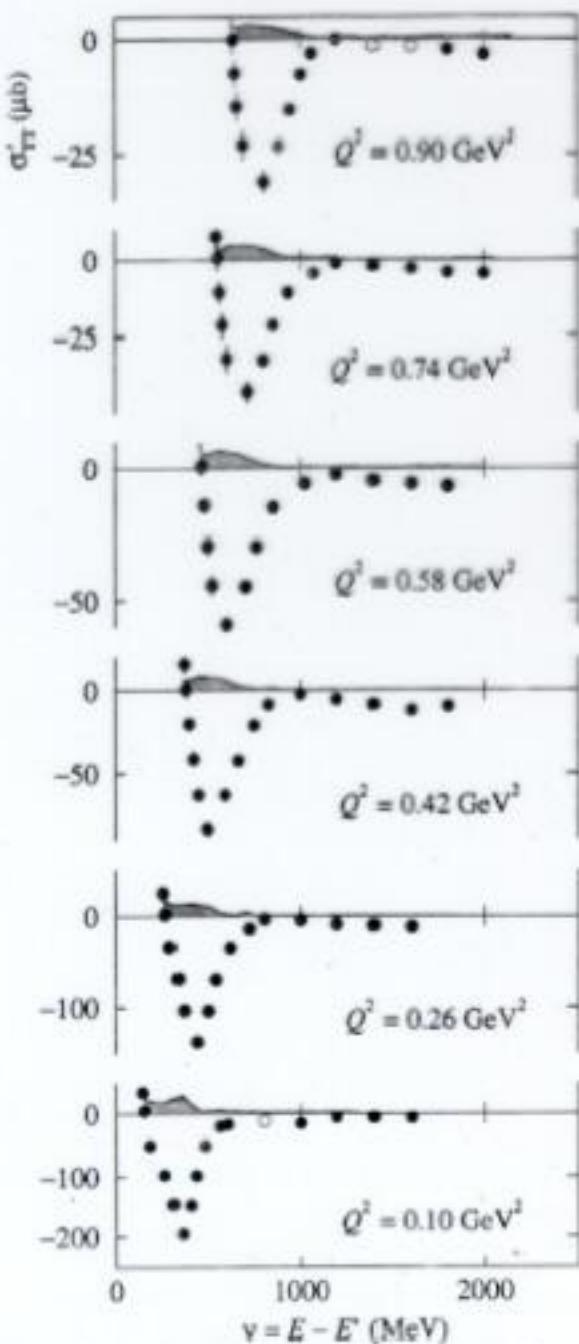


FIG. 2.  $\sigma'_T J$  is plotted as a function of energy loss  $\nu$  for each of six values of constant  $Q^2$ . The points shown with solid (open) circles were determined by interpolation (extrapolation).

$\Delta_{1232}$  resonance, which decreases in magnitude with increasing  $Q^2$ . The error bars represent the uncertainty due to statistics, and the grey bands indicate the uncertainty due to systematic errors, which in addition to those shown in Fig. 1, include a contribution from interpolation and extrapolation.

The extended GDH integral was computed for each

value of  $Q^2$  according to eq. 1 using limits of integration extending from the nucleon pion threshold to a value of  $\nu$  corresponding to  $W = 2.0 \text{ GeV}$ . The results are given in Table I. Before plotting our results, we have applied a correction to account for the fact that our neutron was embedded in a  ${}^3\text{He}$  nucleus using a calculation due to Ciofi degli Atti and Scopetta [27]. This procedure introduces an additional 5% systematic uncertainty in our result. Our results for  $I(Q^2)$  for the neutron, with the integration covering roughly the resonance region, are shown in Fig. 3 using open circles. The error bars, when visible, represent statistical uncertainties only, and the systematic effects are shown with the grey band. We have made an estimate of the unmeasured strength in  $I(Q^2)$  for the region  $4 \text{ GeV}^2 < W^2 < 1000 \text{ GeV}^2$  using the parameterization of Thomas and Bianchi [29] ( $1000 \text{ GeV}^2$  was the highest value considered in their paper). The solid squares have this estimate included, and an estimate of the theoretical uncertainty has already been included in the systematic error shown.

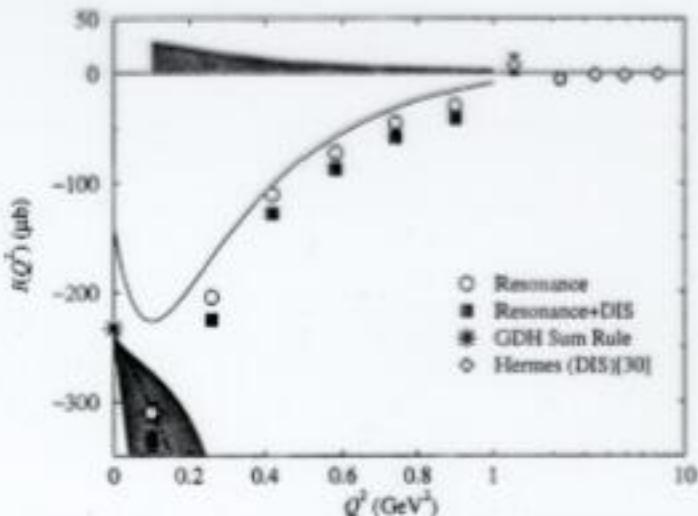


FIG. 3. Our measurements for  $I(Q^2)$  vs.  $Q^2$ , both with and without an estimate of the DIS contribution. Also shown with a dotted (dot-dashed) line are the  $\chi$ PT calculations of ref. [12] (refs. [13] and [14]). The calculation of ref. [11], based largely on the MAID model, is shown with a solid line. We have included data from HERMES [30], and to avoid compressing our horizontal scale, we have adopted a semi-log scale for  $1 \text{ GeV}^2 < Q^2$ .

$Q^2$ (GeV²)	$I_{\text{DDH}}$ (μb)	Statistical (μb)	Systematic (μb)
0.10	-223.76	6.18	23.68
0.26	-156.52	3.01	13.58
0.42	-88.73	2.10	7.46
0.58	-59.56	1.51	4.56
0.74	-37.96	1.43	3.14
0.90	-23.63	1.00	2.09

TABLE I. Measured values for  $I(Q^2)$  prior to nuclear corrections together with statistical and systematic errors.