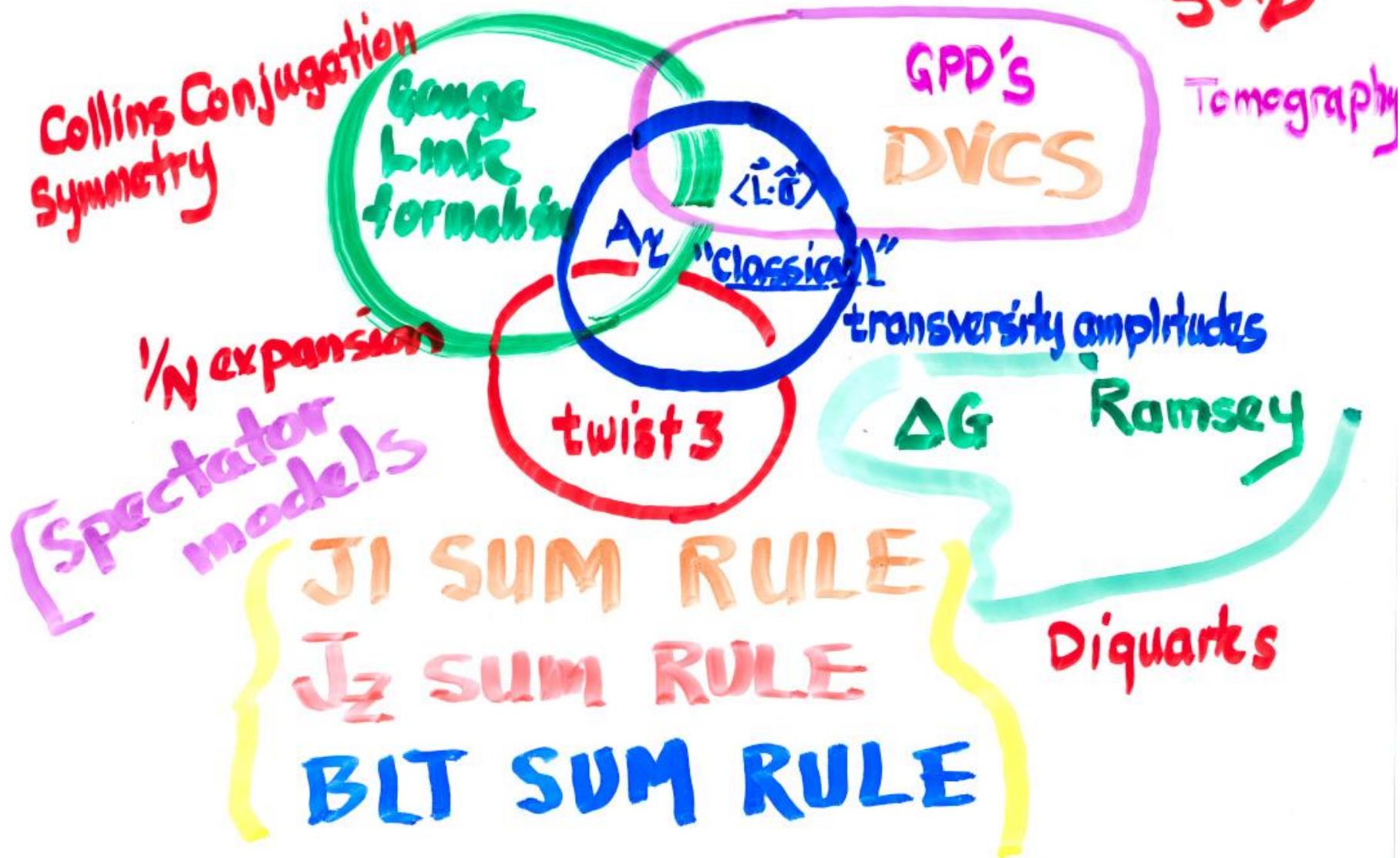


|| Spin-orbit dynamics ||



Angular Momentum Sum Rules

[a consumer's guide]

$$J_i = J_i = \sum_q (J_{iq} + J_{ig}) = \sum_a \left\{ H_a(x, 0, 0) + E_a(x, 0, 0) \right\}$$

$$\text{BRS Rotating } J_z = \frac{1}{2} = \frac{1}{2} \sum_q \hat{s}_q \cdot \hat{e}_z + \hat{s}_g \cdot \hat{e}_z + \sum_a \langle \vec{L}_a \cdot \hat{e}_z \rangle \quad \hat{\sigma}_p \cdot \hat{e}_z = 1$$

$$\text{BLT } J_y = \frac{1}{2} = \frac{1}{2} \sum_q \hat{s}_q \cdot \hat{e}_y + \sum_a \langle \vec{L}_a \cdot \hat{e}_y \rangle \quad \hat{\sigma}_p \cdot \hat{e}_y = 1$$

These contain Independent Information

Example from Georgi Manchuk

azimuthal symmetry

$$J_z = \frac{1}{2} = \frac{1}{2} \Delta \mathcal{E}_0(\mu^2) + \Delta G(M^2) + \sum_a \langle \vec{L}_a \cdot \hat{\sigma}_p(\mu^2) \rangle \quad \text{Observable?}$$

$$J_y = \frac{1}{2} = \frac{1}{2} \Delta \mathcal{E}_T(\mu^2) + \sum_a 2 \int dx d^2 k_T \Delta^N G_{a/T}^{front}(x, k_T(x); \mu^2)$$

not direct observables

(represent intrinsic props)

Orbital Ang. Momentum & $\Delta G(x,t)$

Y. Binder
G. Ramsey

$$A_0(x) = \frac{\partial/\partial t \Delta G(x,t)}{\partial/\partial t G(x,t)}$$

solve
LO & NLO
DGLAP!

$$A(x,t) = A_0(x) + E(x,t)$$

$$\Delta G(x,t) = A_0(x)G(x,t) + \Delta G_E(x) \quad \text{with } \Delta G_E(x) = E(x,t)G(x,t)$$

$$\Delta G(x,t_1) - \Delta G(x,t_0) = A_0(x)[G(x,t_1) - G(x,t_0)]$$

all t -dependence and all perturbatively generated orbital angular momentum - Ratcliffe

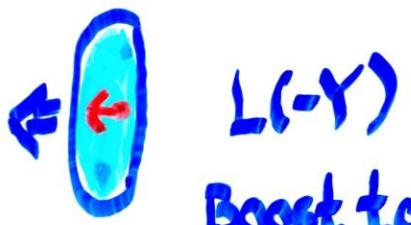
$\Delta G_E(x)$ describes nonperturbative effects

Ratcliffe - Subtracted Sum Rule

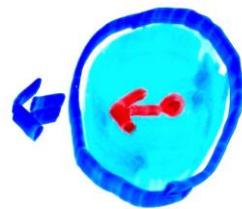
ΔG TESTS Low-Energy Chiral Dynamics!

Transversity & Orbital angular momentum

T. Binder
G. Ramsey



Boost to
Rest Frame



Rotate by
π/2



Boost to
Original Frame



only the S-wave component of the appropriate helicity amplitude survives!! The $L \neq 0$ components contribute to Boer, Mulders Functions instead of transversity dist'n's.

$$\langle p+|Q_L|q+\rangle = \langle Q_0 \rangle + \sum_{L=1} \langle Q_L + Q_{-L} \rangle$$

Transversity
 $|Q_0|^2$

Boer, Mulders
 $\sum |Q_L|^2 (-)^L$