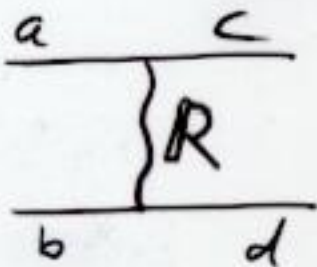


Forward neutrons and photons  
in pp collisions

Boris Kopeliovich

# Regge theory recollections

## • Binary reactions



$$A_R^{ab \rightarrow cd}(s, t)$$

$$= h_R(t) \eta_R(t) \left( \frac{s}{s_0} \right)^{\alpha_R(t)}$$

Residue function  
spin structure

Phase factor

Energy  
dependence

$$h_R(t) = h_0(t) + h_1(t) \vec{\sigma} \cdot \vec{n}$$

$$\eta_R(t) = \begin{cases} i - \cotg \frac{\pi \alpha_R(t)}{2} \\ -i - \tng \frac{\pi \alpha_R(t)}{2} \end{cases}$$

positive signature ( $P, f, a_2$ )

negative signature ( $\rho, \omega$ )

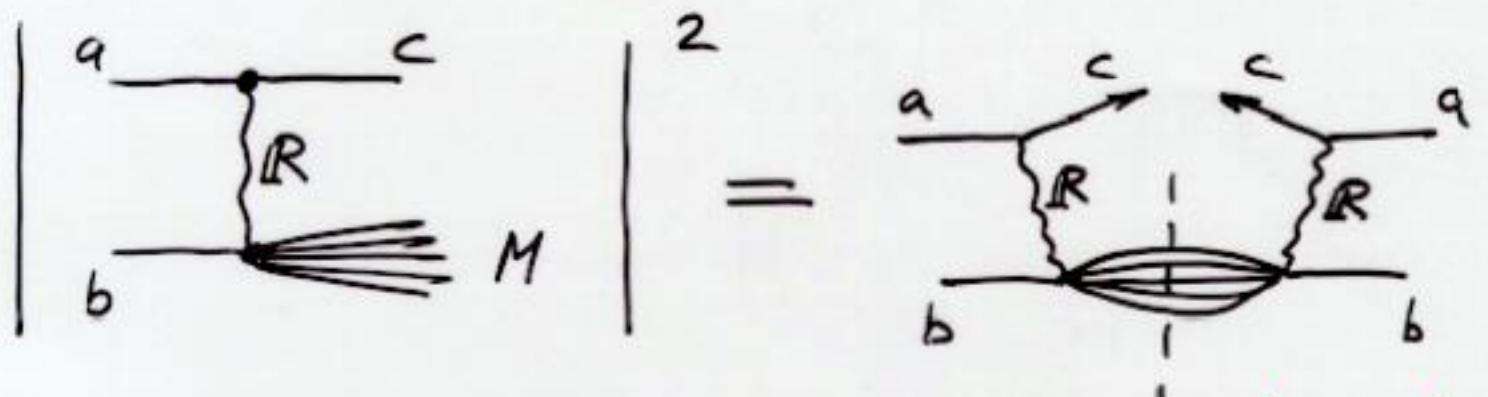
$$\alpha_R(t) = \alpha_R^0 + \alpha_R' t$$

$$\alpha_P^0 \approx 1.1 ; \quad \alpha_P' = 0.25 \text{ GeV}^{-2}$$

$$\alpha_R^0 \approx 0.5 ; \quad \alpha_R' \approx 0.9 \text{ GeV}^{-2}$$

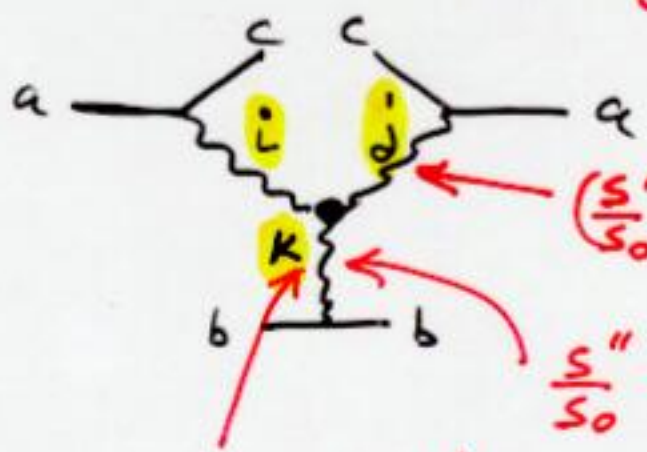
$$\underline{R = \omega, f, \rho, a_2}$$

● Inclusive hadron production in the beam fragmentation region ( $X_F \gtrsim 0.1$ )



Unitarity cut

optical theorem



$$\left(\frac{S'}{S_0}\right) = \frac{S}{M^2} = \frac{1}{1-X_F}$$

$$\frac{S''}{S_0} = \frac{M^2}{S_0} = (1-X_F) \frac{S}{S_0}$$

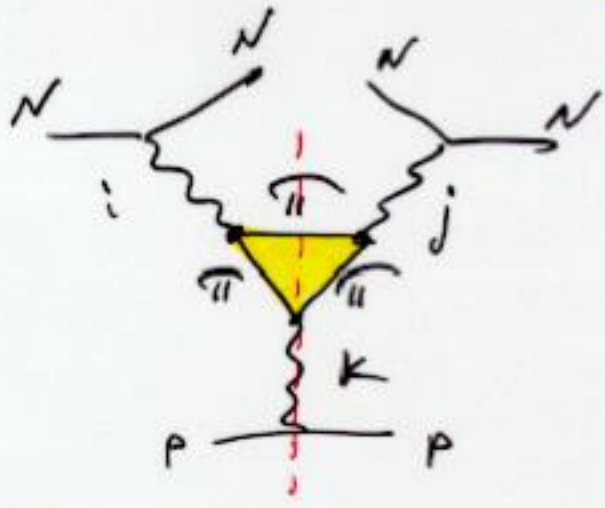
Imaginary part of forward scattering amplitude

$$\frac{d\sigma}{dt dx_F}^{ab \rightarrow cX} = \sum_{i,j,k} G_{ijk}(t) (1-X_F)^{\alpha_k(0) - \alpha_i(t) - \alpha_j(t)} \times \left(\frac{S}{S_0}\right)^{\alpha_k(0) - 1}$$

Triple-Regge vertices Fitted to data



# OPE model for the triple-Regge couplings



Y. Kazarinov  
I. Lapidus  
I. Potashnikova  
B.K.  
1975

$$G_{ijk}(0) = g_{NNi} g_{NNj} g_{NNk} g_{\pi\pi i} g_{\pi\pi j} g_{\pi\pi k} \eta_i(0) \eta_j(0) I_{ijk}$$

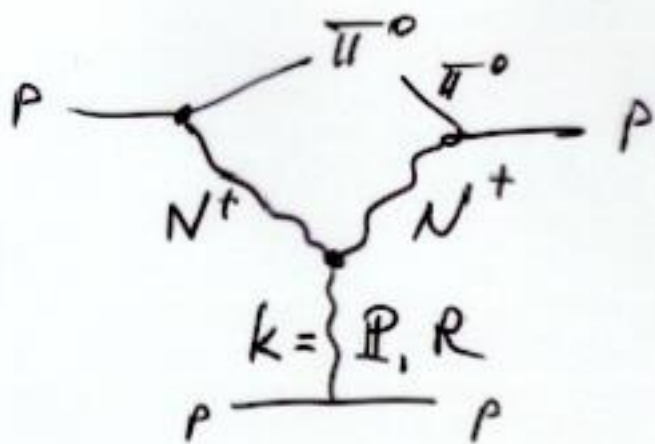
$$I_{ijk} = \frac{3}{(4\pi)^4 s_0} \int_{-\infty}^0 \frac{du}{(m_\pi^2 - u)^2} \left( \frac{m_\pi^2 - u}{s_0} \right)^{\alpha_i(0) + \alpha_j(0)} F(u) \times \int_0^{\frac{-u}{(m_\pi^2 - u)}} d\left(\frac{M_1^2}{M^2}\right) \left(\frac{M_1^2}{M^2}\right)^{\alpha_k(0)}$$

Comparison with the fit to  $pp \rightarrow pX$  data

	$G_{PPP}$	$G_{RRP}$	$G_{PPR}$	$G_{RRR}$	$2\text{Re } G_{RPP}$	$2\text{Re } G_{RPR}$
Theory	4	17	5.4	27.4	10.7	15
Fit	$3.23 \pm 0.35$	$13.2 \pm 0.9$	$2 \pm 1$	$23.6 \pm 5.0$	$5.7 \pm 4.9$	$13.4 \pm 4.5$

units:  $\left(\frac{\text{mb}}{\text{GeV}^2}\right)$

# Forward pions and photons



$$\left. \frac{d\sigma(pp \rightarrow \pi^0 X)}{dx_F dt} \right|_{t=0} = \sum_{P, R} G_{NNK}^{(0)} (1-x_F)^{\alpha_k^0 - 2\alpha_N^0} \times \left(\frac{s}{s_0}\right)^{\alpha_k^0 - 1}$$

At not too small  $1-x_F$  the energy corresponding to the Reggeon  $k$  is very high:  $s'' = M^2 = (1-x_F)s$ .

Therefore, the Pomeron dominates, and

$$\frac{d\sigma(pp \rightarrow \pi^0 X)}{dx_F dt} = G_{NNP}^{(0)} (1-x_F)^2$$

since  $\alpha_N^0 \approx -0.5$

$$x_F^{\bar{p}} \approx 2 x_F^{\gamma}$$

$$\frac{d\sigma(pp \rightarrow \gamma X)}{dx_F dt} \Big|_{t=0} \propto (1 - 2x_F)^2$$

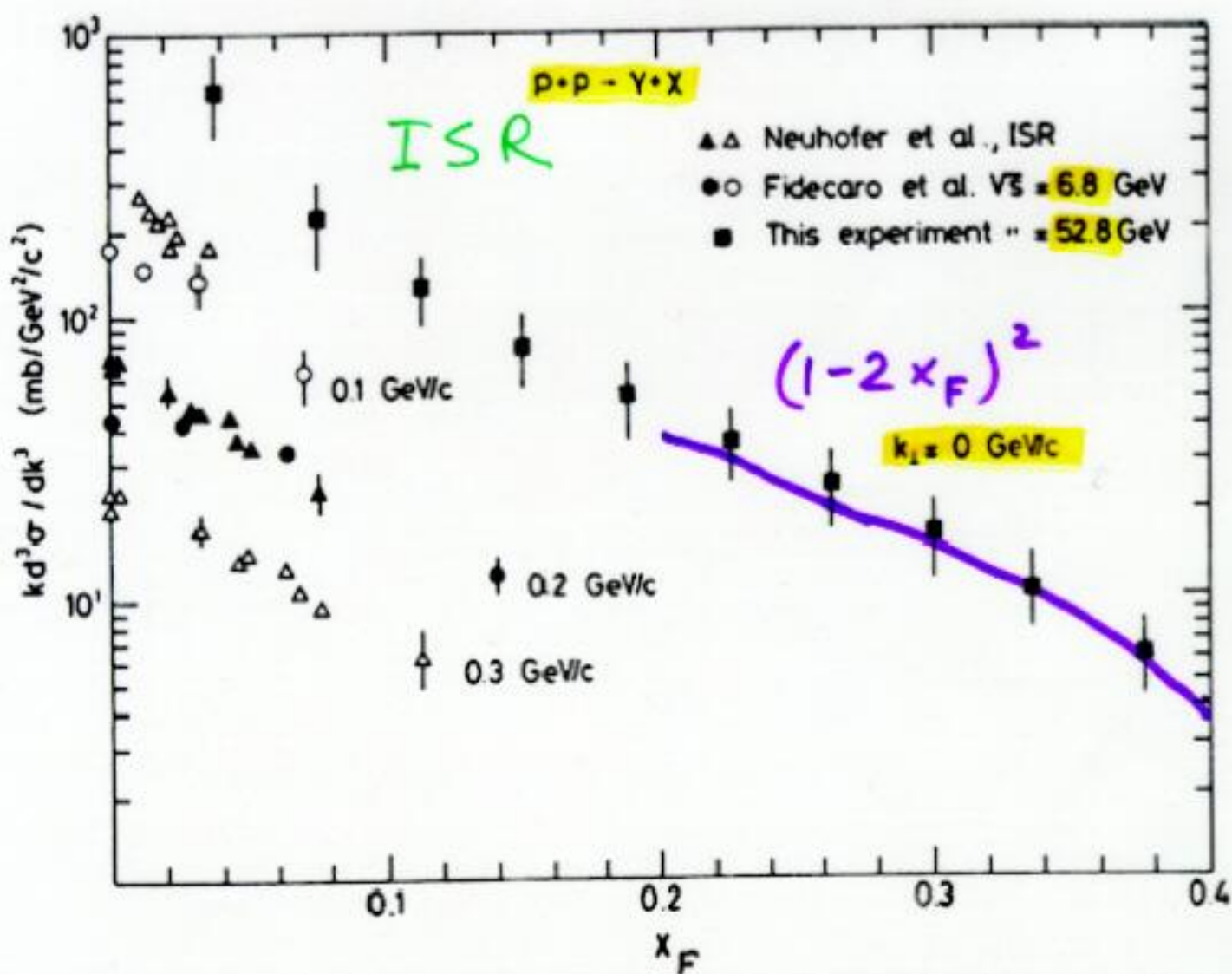
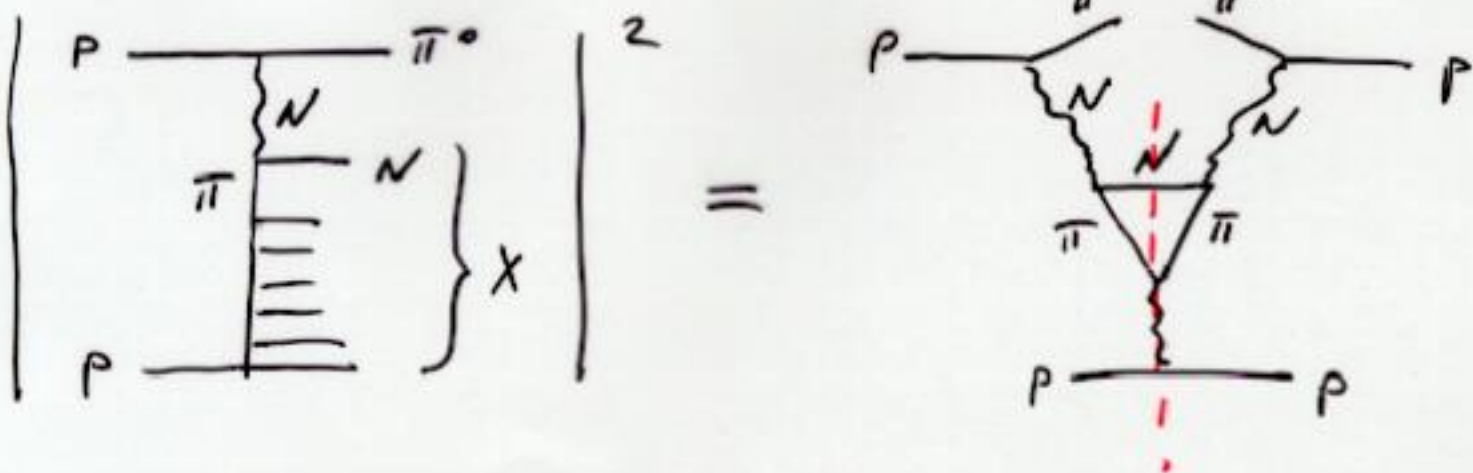


Fig. 4. Invariant cross sections for photon production. The data of this experiment were taken at  $\sqrt{s} = 52.8$  GeV.



# $A_N (pp \rightarrow \pi^0 X)$



$$A_N^{pp \rightarrow \pi^0 X}(s, t, x_F) \approx \frac{2}{3} A_N^{p\pi^- \rightarrow \pi^0 n}(s' = \frac{s_0}{1-x_F}, t)$$

$$+ \frac{1}{3} A_N^{p\pi^0 \rightarrow \pi^0 p}(\frac{s_0}{1-x_F}, t) + (\text{corrections for } \Delta \text{ production})$$

At fixed  $x_F$  the asymmetry is independent of energy.

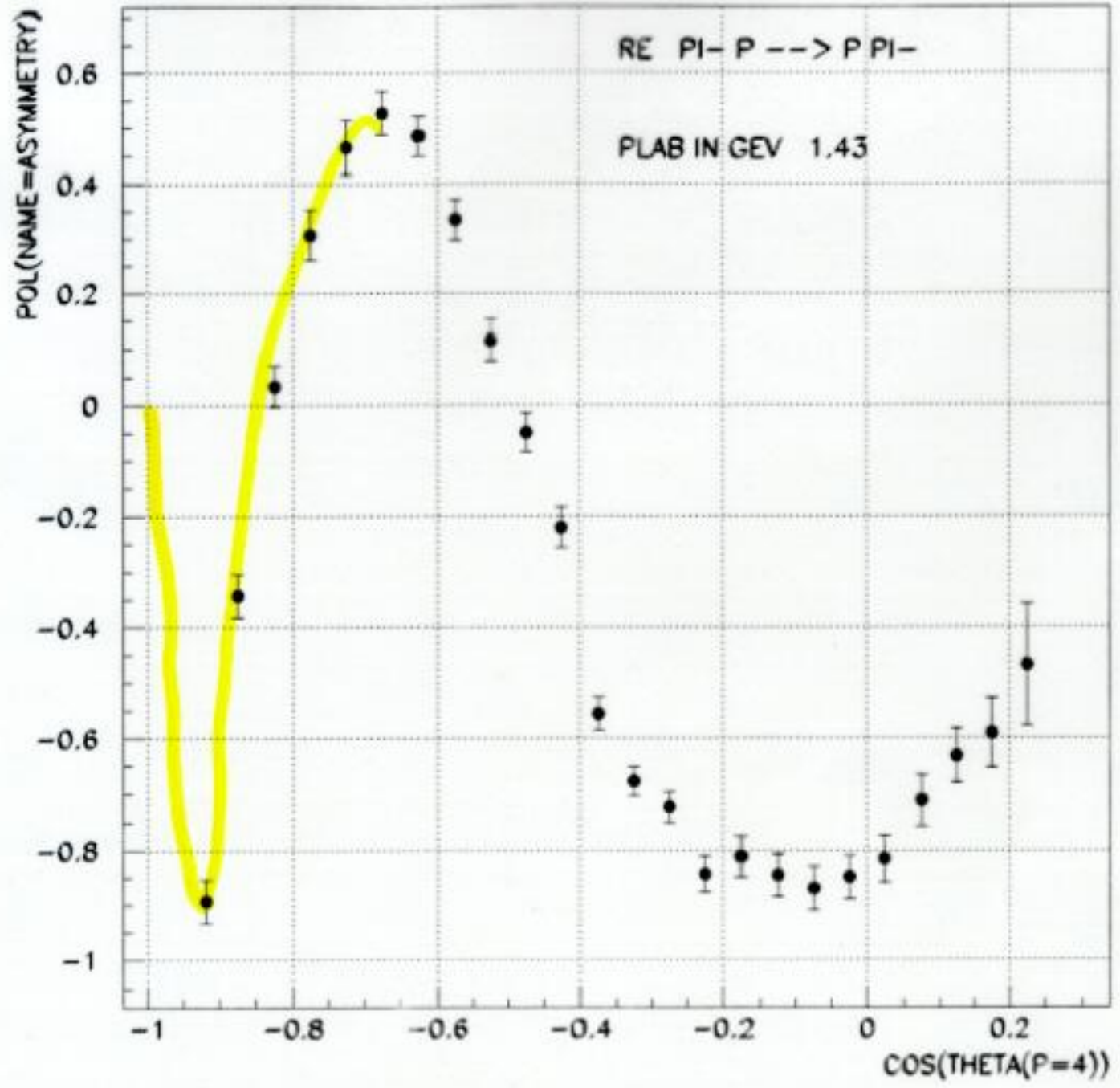
**Feynman scaling,**

This is a general statement for all inclusive reactions ( $pp \rightarrow \Lambda X, \dots$ )

ALEKSEEV 90 NP B348,257

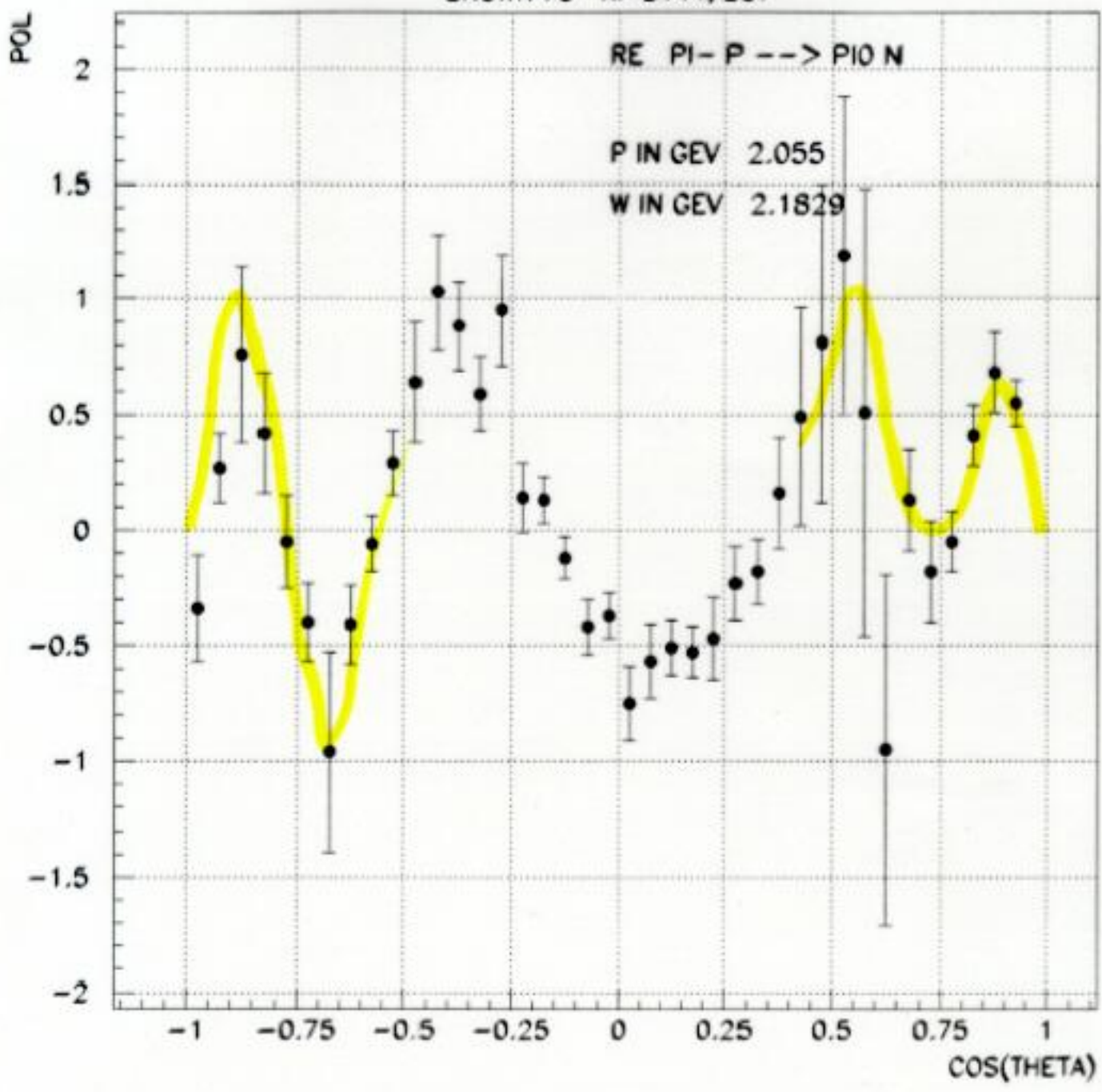
RE  $\pi^- p \rightarrow p \pi^-$

PLAB IN GEV 1.43

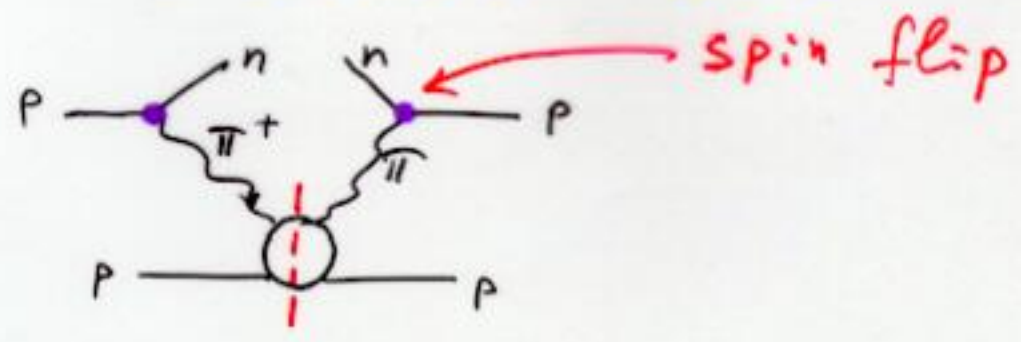




BROWN 78 NP B144, 287



# Forward neutrons



$$\frac{d\sigma}{dx_F dt} \Big|_{\pi}^{PP \rightarrow nX} = \frac{2g_{\pi NN}^2}{(4\pi)^2} \sigma_{tot}^{\pi^+ p} \frac{-te^{R^2 t}}{(m_{\pi}^2 - t)^2} (1-x_F)^{1+2\alpha'_{\pi}|t|}$$



$$\frac{d\sigma}{dx_F dt} \Big|_R^{PP \rightarrow nX} = \frac{2}{(4\pi)^2} [g_{\rho}^2 e^{R_{\rho}^2 t} + g_{a_2}^2 e^{R_{a_2}^2 t}] \sigma_{tot}^{RP} |\eta_R|^2 \times (1-x_F)^{2\alpha'_R |t|}$$

$$\sigma_{tot}^{RP} \approx \sigma_{tot}^{\pi p}; \quad \frac{g_{\rho}^2}{4\pi} = 0.18 \text{ GeV}^{-2}; \quad \frac{g_{a_2}^2}{4\pi} = 0.4 \text{ GeV}^{-2}$$

$$R_{\rho}^2 = 2 \text{ GeV}^{-2}; \quad R_{a_2}^2 = 1 \text{ GeV}^{-2}; \quad |\eta_R|^2 \approx 2$$

For DIS one should just

replace  $\sigma_{tot}^{\pi p} \Rightarrow \sigma_{tot}^{\gamma^* p} = \frac{2\pi\alpha^2}{Q^2} F_2^{\bar{p}}(x, Q^2)$

$\pi$

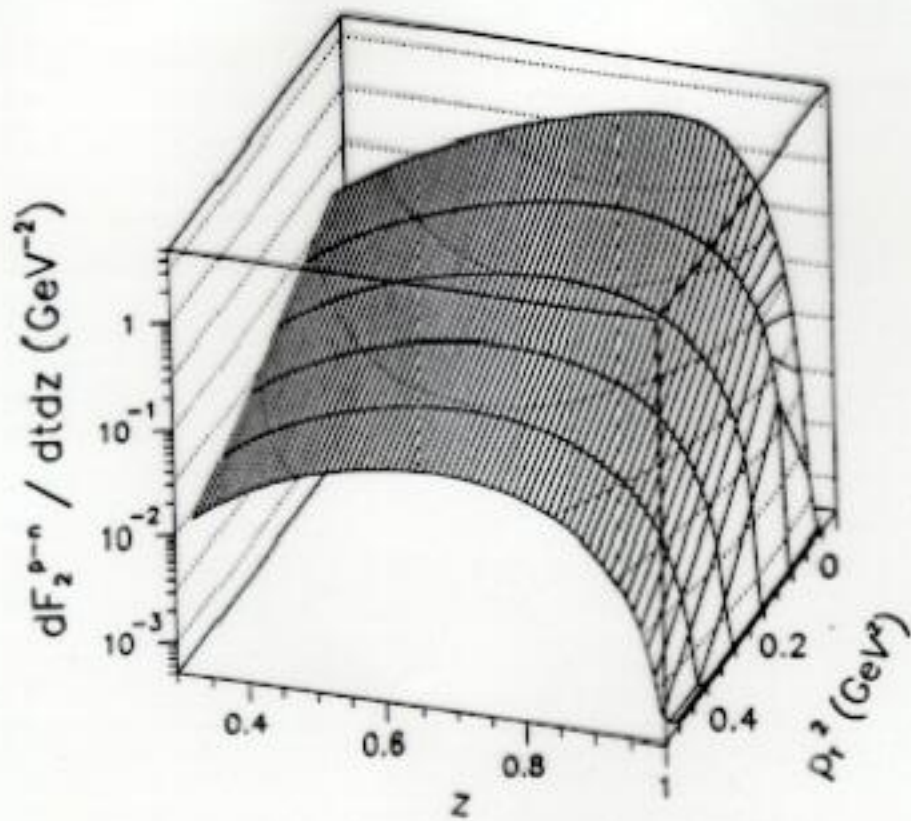


Fig. 3. The neutron electroproduction cross section, corresponding to the pion-pole diagram in Fig. 1a, versus  $p_T^2$  and  $z$

I. Potashnikova  
B. Povh  
B.K.  
1996

$\rho + a_2$

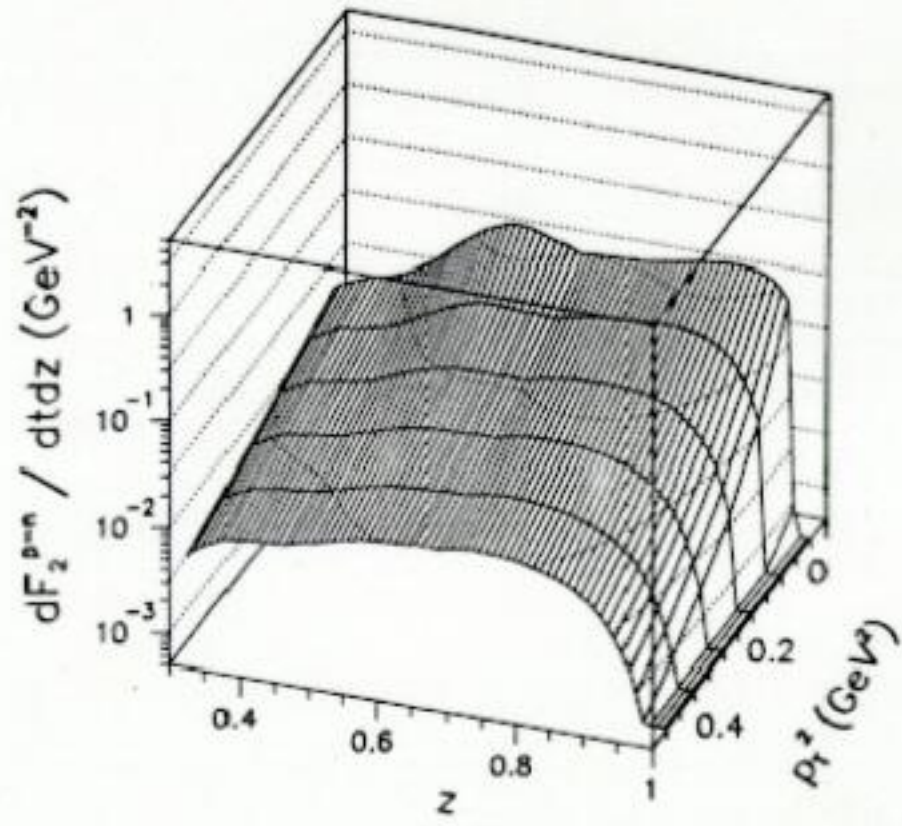


Fig. 4. The neutron electroproduction cross section, corresponding to the pion-pole diagram in Fig. 1b, versus  $p_T^2$  and  $z$





pp → nX

W. Flauger, F. Mönning / Inclusive zero-angle neutron spectra

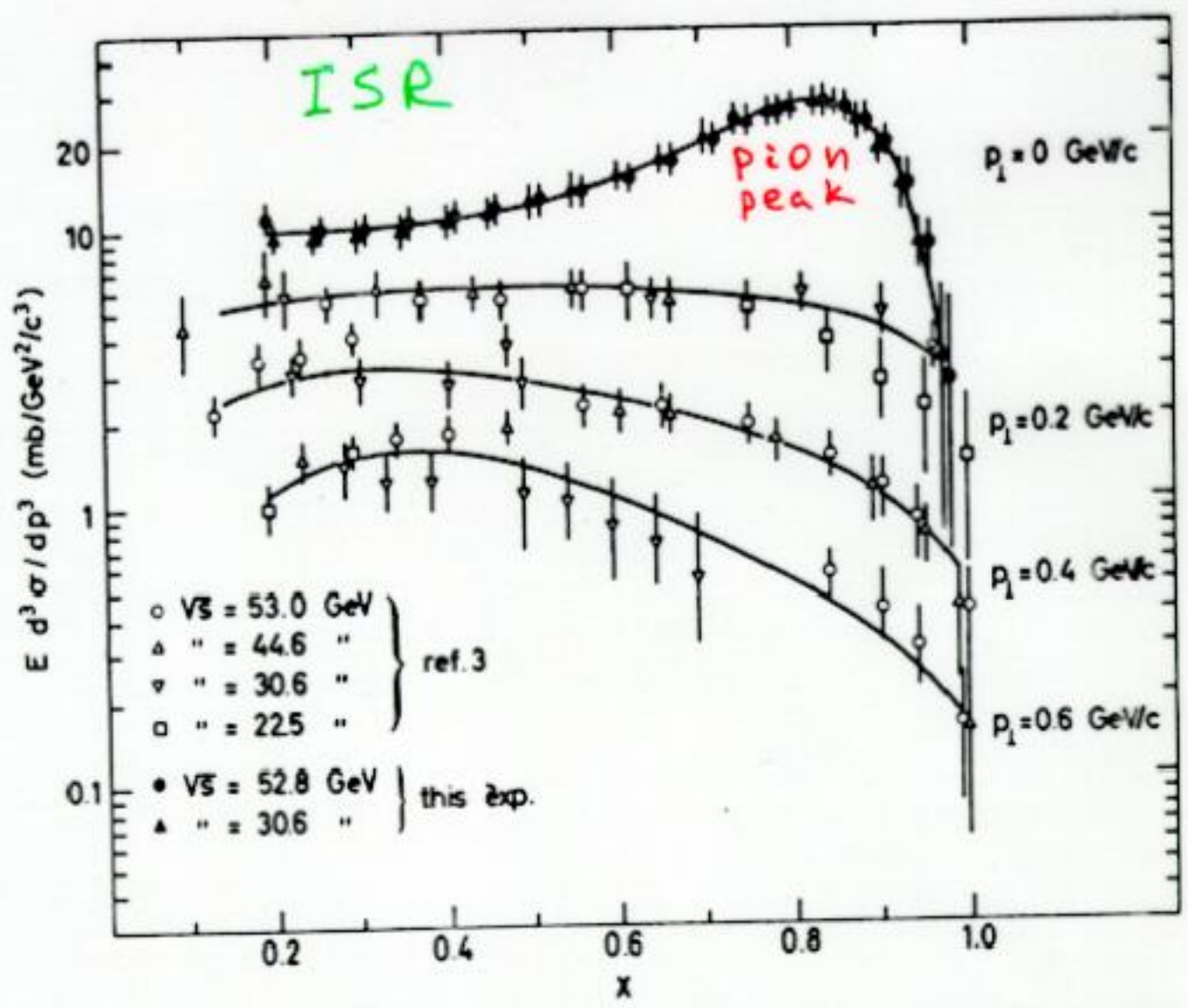


Fig. 3. The invariant cross sections for neutron production as a function of the scaling variable  $x = p_{\parallel}/p_{\text{max}}$ . The lines are hand drawn to guide the eye.

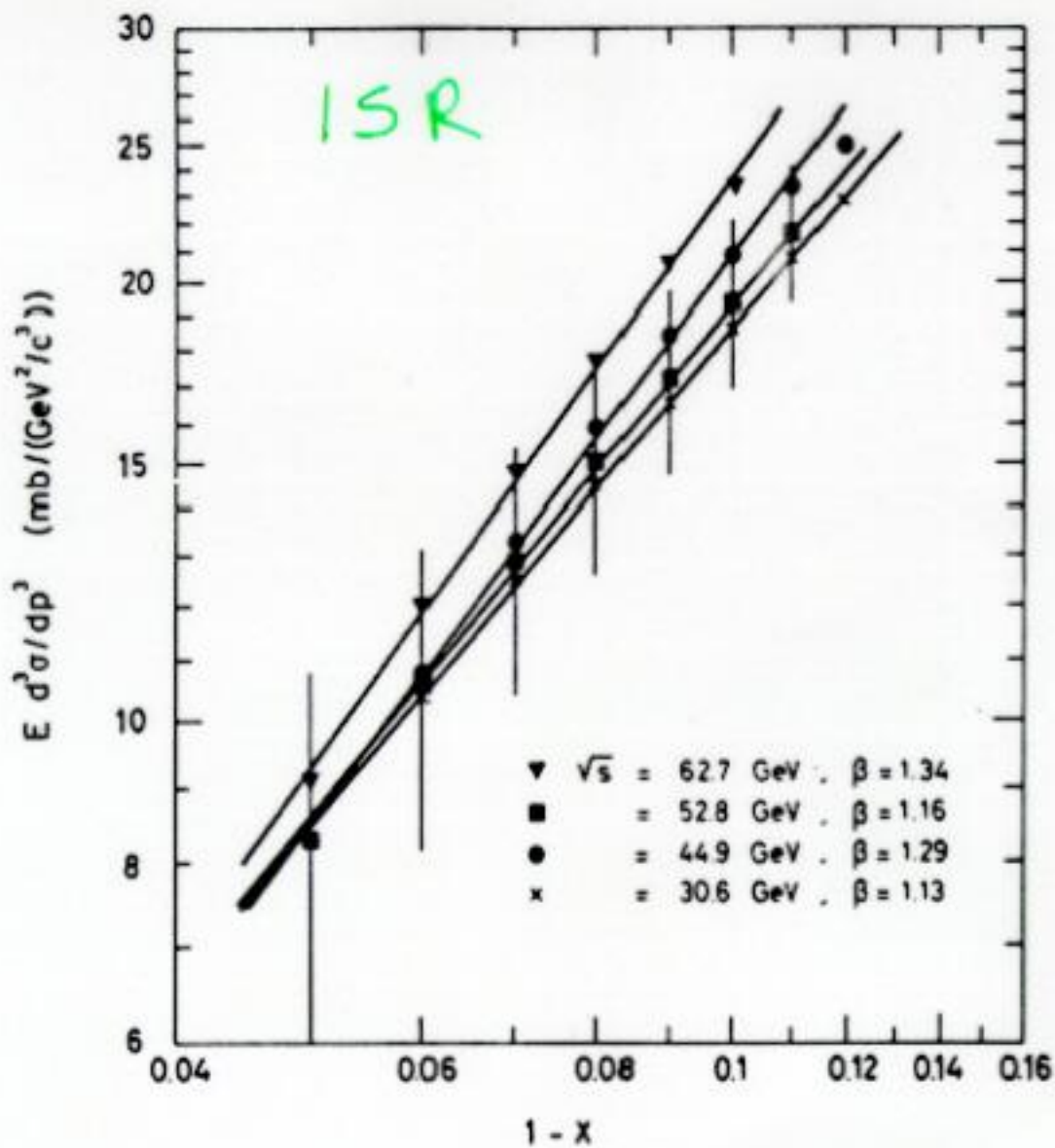


Fig. 5. The neutron cross sections as a function of  $M^2/s \approx 1 - x$  for the momentum transfer squared  $t \approx 0$ .

$$\left. \frac{d\sigma}{dx_F dt} \right|_{t=0} \propto (1-x_F)^\beta$$

$$\beta = 1 - 2\alpha_{\text{eff}}^0$$

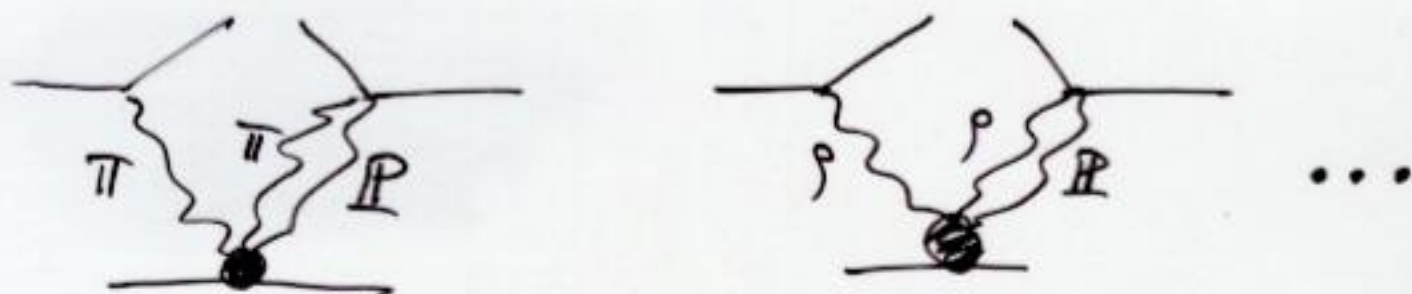
$$\alpha_{\text{eff}}^0 = -0.11 \pm 0.15$$

Consistent  
with pion  
 $\alpha_{\pi}^0 = 0$

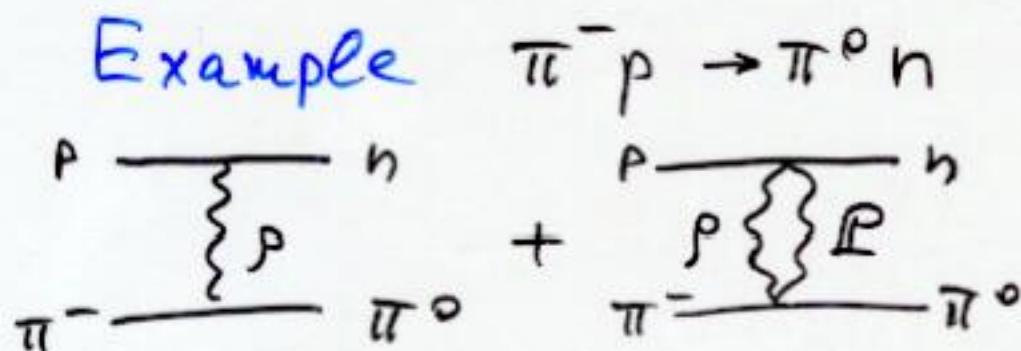


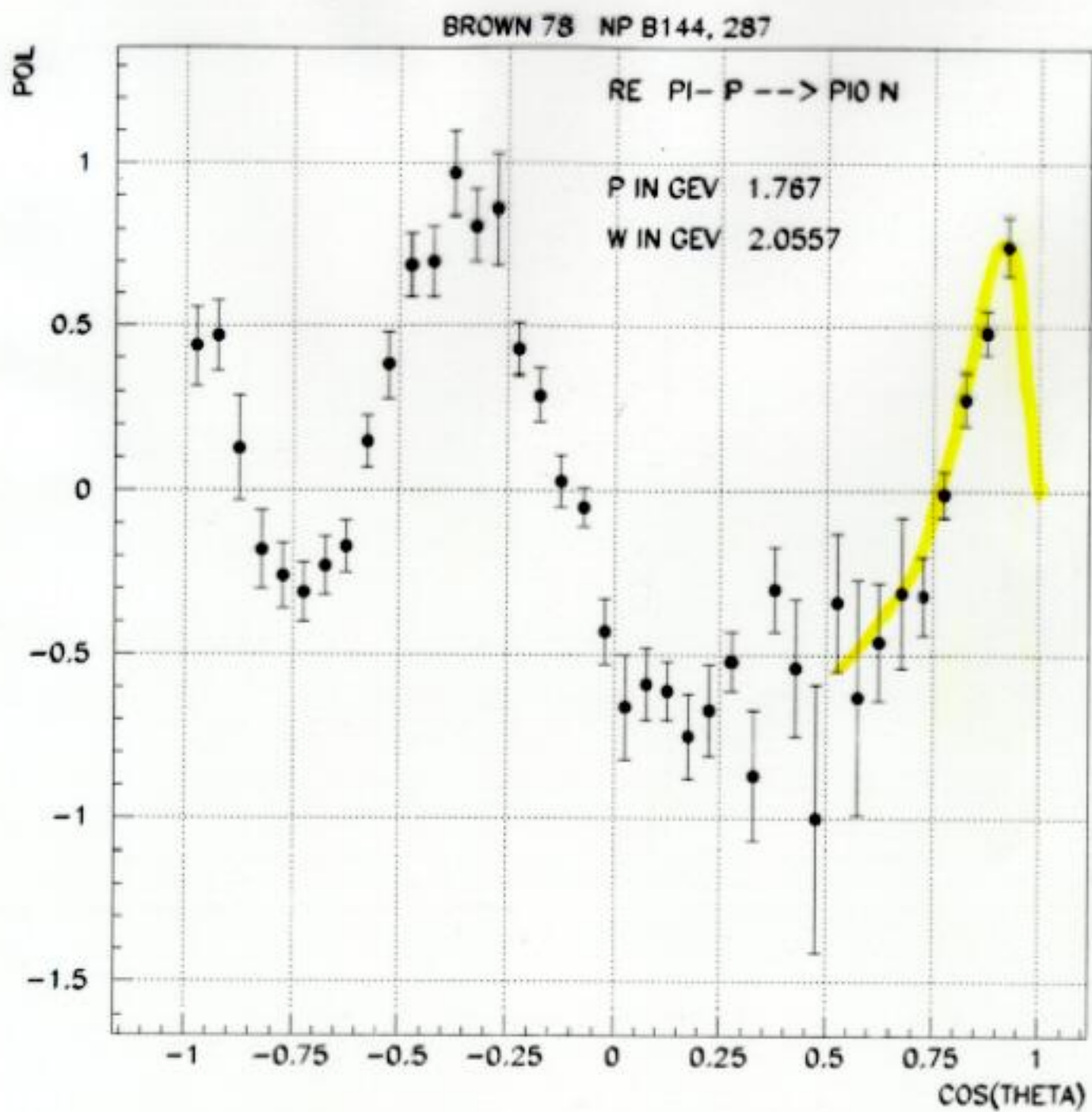
# $A_N (pp \rightarrow nX)$

all the dominant contributions are dominated by the spin-flip parts. Asymmetry is due to interference between Regge poles and cuts



The known effects are strong at medium energies  $S' = \frac{S_0}{1-X_F} \approx 2 \text{ GeV}^2$







## Conclusions

- Polarization effects in inclusive reactions, as well as the cross section, are independent of energy (with some corrections)
- Asymmetry in  $pp \rightarrow \pi^0(f)X$  might be small due to the strong oscillating  $t$ -dependence and opposite signs of  $A_N$  in different channels
- Neutron production is dominated by pion exchange. A large  $A_N$  is expected from  $\pi$  and  $\pi P$  (absorptive corrections) interference.